Low Voltage Clocking Methodologies for Nanoscale ICs

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Abstract of the Dissertation

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Power consumption has emerged as a key design objective for almost any application. Low swing/voltage clock distribution was proposed in earlier work as a method to reduce power consumption since clock networks typically consume a significant portion of the overall dynamic power in synchronous integrated circuits (ICs). Existing works on low voltage clocking, however, suffer from multiple issues, making these approaches impractical for industrial circuits. For example, most of the existing studies sacrifice performance when lowering the supply voltage of a clock network, such as clock networks developed for near-threshold computing. The primary objective of this dissertation is to develop a low voltage clocking methodology without degrading circuit performance (operating frequency) or clock network characteristics (such as skew and slew). This objective is achieved through several circuit and algorithmic innovations.

A novel D flip-flop (DFF) cell that can reliably operate with a low voltage clock signal and a nominal voltage data signal is proposed. Contrary to existing approaches where the last stage of the clock network operates at nominal voltage, the proposed cell enables low voltage clock operation throughout the entire clock network, thereby maximizing power savings. Furthermore, a similar clock-to-Q de-lay is maintained to satisfy the same timing constraints. Simulation results demonstrate that when the clock voltage is scaled to 70% of the nominal supply voltage, the proposed DFF cell achieves up to 53% power savings at the expense of approximately 50% increase in cell-level physical area. At chip-level, the increase in area is approximately 15%.

At low supply voltages, satisfying the slew constraint becomes highly challenging due to reduced drive ability of the clock buffers. A slew driven-clock tree synthesis (CTS) methodology, referred to as SLECTS, is proposed to satisfy tight slew constraints at scaled supply voltages. Contrary to existing CTS methods that are primarily delay/skew based and slew is considered only during post-CTS optimization, in the proposed approach, slew constraint is integrated into the critical steps of the synthesis process (such as merging clock tree nodes, defining routing points, and handling long interconnects). For an industrial 4-core application processor with approximately 1 million gates and implemented in 28 nm fully depleted silicon-on-insulator (FD-SOI) CMOS technology, the proposed slew-driven CTS methodology achieves up to 15% reduction in clock tree power while producing satisfactory skew and slew characteristics. Furthermore, contrary to the vendor tool that exhibits slew violations, the proposed approach satisfies tight slew constraints. When the proposed DFF cell is combined with the proposed CTS methodology, up to 48% reduction in overall clocking power is achieved under similar performance constraints at the expense of 15% increase in area.

In clock trees with highly aggressive design constraints, selective low voltage clocking was considered to satisfy the tight constraints. A novel level-up shifter with dual supply voltage is proposed to enable such operation. Simulation results demonstrate that the proposed level shifter achieves 43% and 36% reduction in, respectively, transient power and leakage power as compared to a conventional cross-coupled level shifter, while consuming 9.5% less physical area.

Clock gating is an effective and common technique to reduce the switching power of the clock networks. Clock signals arrive at clock gating cells earlier than sinks, which reduces the timing slack of *Enable* paths. A useful skew methodology for gated low voltage clock trees is proposed to relax the timing constraints of *Enable* paths. The methodology is evaluated using the largest ISCAS'89 benchmark circuits. The results demonstrate an average 47% increase in the timing slack of the *Enable* path.

The design methodologies proposed in this dissertation facilitate low voltage clocking for high performance industrial circuits. Significant reduction in clock power is achieved without degrading clock frequency and primary clock constraints such as skew and slew. The proposed methodologies were integrated into a conventional design flow and demonstrated using large scale industrial circuits.

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Chapter 1

Introduction

Power consumption has become a primary concern for almost any application due to increased design complexity, higher integration, and difficulty in scaling the power supply voltage [5–10]. A clock distribution network consumes approximately 20-45% of total on-chip power and approximately 90% of this power is consumed by the flip-flops and last branches of a clock tree [11–13]. This power dissipation is the result of increased pipelining in an integrated circuit (IC) which has led to an increase in the number of flip-flops and hence the overall interconnect length of the clock network [14]. Clock gating [15–18] is an effective technique to reduce the clock network dynamic power consumption by deactivating clock signals for idle sinks. Dynamic power consumption is determined by,

$$P_{dynamic} = \alpha C V_{supply}^{2} f, \qquad (1.1)$$

where α is the switching activity factor, *C* is the load capacitance, V_{supply} is the supply voltage, and *f* is the operating frequency. Switching activity factor is equal to

one in an ungated clock network. To reduce dynamic power consumption, modern ICs are heavily clock gated, thereby reducing the switching activity. Another wellknown approach to minimize the overall on-chip power dissipation is to reduce the supply voltage [19–21]. For example, near-threshold computing has received considerable attention to achieve optimal energy efficiency [22]. A reduction in supply voltage, however, degrades IC performance, particularly when the nominal supply voltages are low [19]. Low swing signaling has also been investigated to reduce dynamic power consumed by long interconnects [23]. This approach has been extended to clock networks due to high clock net capacitance [24–26]. Clock networks operating at near-threshold voltages have also been investigated [27–29].

Existing works on low swing/voltage clock networks, however, are effective primarily for low power applications that do not demand high performance. Achieving a reliable low swing clock network *without* sacrificing performance is challenging due to the following issues: 1) the interface between a low swing clock signal and flip-flop may increase clock-to-Q delay, thereby reducing the timing slack within the data paths while also increasing power consumption, 2) clock buffers operating at a lower voltage increase the insertion delay along the clock path, causing higher clock skew and degraded slew, and 3) timing slack of *Enable* paths is reduced in gated clock trees operating at a lower voltage. These three challenges are described more in detail in Chapter 2.

In this thesis, these primary issues are addressed through both circuit and algorithmic innovations, as shown in Fig. 1.1, making low swing clocking a practical power reduction strategy for both low power and high performance applications. Circuit-level novelties include a novel D-flip-flop (DFF) cell and a novel level-up shifter. The proposed DFF cell achieves similar clock-to-Q delay as traditional full



Figure 1.1: Primary components of the proposed low swing clocking methodology.

swing DFF topology while consuming less power. Reliable operation is ensured despite a low swing clock signal and a full swing data signal. The proposed levelup shifter enables selective low swing operation for high performance applications. The proposed clock skew scheduling algorithm maximizes circuit performance and increases the timing slack of *Enable* paths, an important issue in low voltage clock trees. A slew driven clock tree synthesis methodology is also proposed to simultaneously satisfy the skew and slew constraints while maintaining the same performance as in full swing operation.

The rest of the thesis is organized as follows. Background on clock distribution and existing works on low swing/voltage clocking are summarized in Chapter 2. Design challenges related to low voltage clock networks are also described. The proposed flip-flop is presented in Chapter 3. The proposed level-up shifter for selective low swing clocking is introduced in Chapter 4. The proposed clock skew scheduling algorithm is described in Chapter 5. The proposed slew-driven clock tree synthesis methodology is presented in Chapter 6. Finally, the thesis is concluded in Chapter 7 with a brief discussion on future directions.

Chapter 2

Background

In a fully synchronous IC, a global clock signal is typically used to ensure the correct movement of data that flow between different registers [11]. To reliably deliver global clock signals to all of the registers, a clock distribution network and its particular characteristics should be investigated. Several clock distribution topologies, the concept of clock skew, and timing constraints are introduced in Section 2.1. When synthesizing a clock distribution network, clock buffers are inserted to balance clock insertion delay and ensure clock signals with fast transition times. Background on clock tree synthesis (CTS) is also provided in Section 2.1.1. Existing works on low swing/voltage clocking are summarized in Section 2.2. Design challenges in low swing/voltage clocking and the proposed solutions to these challenges are described in Section 2.3.



Figure 2.1: A simple synchronous system.

2.1 Clock Distribution Networks

A simple synchronous system with two registers is shown in Fig. 2.1. The launch and capture elements can be an edge-triggered flip-flop or level sensitive latch [30]. The combinational circuit performs logic computations. Two registers and the combinational logic circuit compose a timing path from the launch element to the capture element. Assuming that both launch and capture elements are rising edge-triggered flip-flops, the register changes its output state only after the rising edge of the clock signal arrives. Once a rising edge of the clock signal arrives, the output of the launch element latches the input data signal. The signal then propagates through the logic circuit, and arrives at the input of the capture element. After the output of the capture element during the following rising edge of the clock signal. Thus, the launch and capture elements ensure the correct order of the data flow. One entire clock period is available for the data to be latched into the launch element, propagate through the combinational logic, and arrive at the input of the capture of the capture element.

synchronized with a global periodic clock signal.

In addition to the launch/capture elements and combinational logic, Fig. 2.1 also includes a clock generator which is typically a phase-locked loop (PLL). A PLL generates the global clock signal with a specified clock frequency. A clock distribution network also exists to deliver the clock signal from the output of the clock generator to each launch and capture elements in a synchronous IC. Since the clock signal is vital to the operation of a fully synchronous IC, significant attention is given in distributing the clock signal to each sequential element throughout the chip. Since a clock distribution network synchronizes all of the data that flow among different launch and capture elements, clock network should be reliable and stable to ensure the correctness of the circuit operation.

Clock signals have unique characteristics. A clock signal typically drives a large amount of capacitive load, travels across the entire die and operates with the highest speed within the entire IC [11, 31]. Since the clock signal provides timing reference for data signals, it should have a fast signal transition time (*i.e.*, short slew). Furthermore, as technology scales, interconnects have become significantly more resistive, making the design of clock distribution networks more challenging. Satisfying the slew constraint has particularly become more difficult. A large number of clock buffers is typically inserted throughout the clock network to satisfy the slew constraint [32].

Due to long interconnects and clock buffers, clock signals require a certain amount of time to reach the launch/capture elements. This propagation delay is referred to as clock insertion delay. Differences in the clock insertion delay of various launch/capture elements can limit the maximum performance of the entire chip as well as create catastrophic race conditions where an incorrect data signal can be latched into a capture element [5]. This difference in the arrival time of the clock signal to different launch/capture elements is denoted as clock skew. A large clock skew can cause timing violations in a circuit.

2.1.1 Clock Tree Topologies

Many different approaches have been developed for designing clock distribution networks in synchronous digital ICs. Physical die area and power dissipation are significantly affected by the clock distribution network. Different requirements, such as clock frequency, clock skew and slew should be considered while deciding on clock network topology. The most common and general approach is buffered clock trees, which are discussed in Section 2.1.1.1. Contrary to asymmetric trees, symmetric trees, such as H-trees, can be used to distribute high speed clock signals. This approach is described in Section 2.1.1.2.

2.1.1.1 Buffered Clock Trees

The most common strategy for distributing clock signals in high complexity ICs is to insert buffer either at the clock source and/or along the clock paths, constructing a tree topology. A typical buffered clock tree is shown in Fig. 2.2. The unique clock source is referred to as the root of the tree. Each register in the tree is referred to as a leaf.

If the internal resistance of the buffer at the clock source is small as compared to the buffer output resistance, a single buffer is typically placed at the root to drive the entire clock network. This strategy requires the clock buffer to have sufficient drive ability to drive the load capacitance of the clock network while satisfying



Figure 2.2: An example of a buffered clock tree.

the clock skew, slew requirements. As technology scales and die area increases, additional clock buffers are inserted. These clock buffers amplify the clock signals degraded by the distributed interconnect impedances and isolate the local clock nets from the upstream load impedances [33]. In Fig. 2.2, the maximum buffer level is five from root to leaf. The number of buffer stages between the clock source and each clocked register depends upon the total capacitive load, in the form of registers and interconnect, and the permissible clock skew [34]. A clock tree after synthesis using a standard design automation tool is illustrated in Fig. 2.3. The circuit is one of the benchmarks from ISCAS'89.



Figure 2.3: An example of a clock tree after synthesis.

2.1.1.2 H-trees

A symmetric H-tree topology is another approach for distributing clock signals. An H-tree is a fractal structure built by drawing an H shape, then recursively drawing H shapes on each of the vertices [35–38], as shown in Fig. 2.4. The clock signal is transmitted to the four corners of the H shape on each recursion. These four identical clock signals provide the clock sources for next recursion. With enough recur-



Figure 2.4: An example of a symmetric H-tree.

sions, the clock signal is delivered to each register from the clock source. Buffer insertion is also applicable on an H-tree to amplify the clock signal. If the clock loads are uniformly distributed across the die, ideally the H-tree can have zero skew. However, variations in process parameters (such as interconnect resistance) and power supply noise produce a nonzero skew H-tree.

In practice, even variations in process and power supply noise are negligible, an H-tree exhibits nonzero skew because the clock loads are typically not uniform since some leaves of the tree have more capacitance than others. Another reason is on-chip obstructions, such as a memory array. An important drawback of H-tree is the increase in interconnect length, which results in larger clock delay and higher power consumption.



Figure 2.5: A typical data path.

2.1.2 Clock Skew

A general data path in a synchronous circuit is shown in Fig. 2.5, where F_i and F_j represent two registers (flip-flops). A combinational circuit connects the two sequentially adjacent registers. Both clock signals originate from the same clock source. A pair of registers are sequentially-adjacent if only combinational logic circuits (no sequential elements) exist between the two registers. C_i and C_j represent the clock signals of the two registers F_i and F_j , respectively. Assume that the propagation delay from clock source to the F_i register is denoted as T_i . A clock distribution network is designed to deliver these clock signals from clock source to each register. Since all of the clock signals originate from the same clock source, the propagation delay T_i can also be considered as clock arrival time to F_i with respect to a universal time reference (clock signal starts propagating from clock source). The difference in clock arrival time between two sequentially adjacent registers is the clock skew. Referring to Fig. 2.5, the clock skew between F_i and F_j is defined as

$$T_{skew,ij} = T_i - T_j, \tag{2.1}$$

where T_i and T_j are arrival times of the clock signals to register F_i and F_j , respectively.



Figure 2.6: Positive and negative clock skews.

In a synchronous circuit, each pair of sequentially adjacent registers forms a single data path. Each such data path has a local clock skew, as in Fig. 2.5. Therefore, global clock skew between registers that are not sequentially adjacent has no effect on the circuit performance and reliability. However, a global clock skew places constraints on the permissible local clock skew.

As defined by (2.1), clock skew between a pair of register (i, j) is polarized since clock signal can arrive register i earlier or later than register j. Fig. 2.6 shows a positive and negative clock skew. Depending on clock skew polarity, it can have different effects on circuit performance and timing constraints.

2.1.3 Timing Constraints Considering Clock Skew

Ideally, the computations in combinational logic circuit should consume an entire clock period [39,40]. However, sequential circuits, such as flip-flops or latches, cause overhead into this entire clock cycle. If the delay of the combinational logic circuit is too large, the capture element will miss its setup time and may sample the wrong data. This violation is called a setup time or max delay failure. This violation can be fixed by reducing the delay of the logic or by increasing the clock period.



Figure 2.7: Two sequentially adjacent registers.



Figure 2.8: Flip-flop max delay constraint with zero clock skew.

A typical data path consisting of two sequentially adjacent registers R1 and R2 is shown in Fig. 2.7. R1 output Q1 flows through combinational logic circuit and feeds R2 data input. Two clock signals for R1 and R2 are denoted as CK1 and CK2, respectively. The max delay timing constraint on the data path from R1 to R2 is shown in Fig. 2.8, assuming zero clock skew. As the rising edge of clock signal



Figure 2.9: Flip-flop max delay constraint with positive clock skew.

CK1 triggers R1, the data at D1 is latched in. It should propagate to R1 output Q1 and through combinational logic circuit to D2, setting up at R2 before the next rising edge of clock signal CK2. To satisfy max delay constraint, all of these events should be completed within one clock period. Therefore, clock period should satisfy

$$T_{clock} \ge t_{c2q} + t_{com} + t_{setup}, \tag{2.2}$$

where T_{clock} , t_{c2q} , t_{com} and t_{setup} represent clock period, clock-to-Q delay, propagation delay of combinational logic circuit and setup time, respectively.

A max delay timing constraint with nonzero skew is depicted in Fig. 2.9. Clock signal arrives R1 later than R2. Therefore, clock skew $T_{skew,12}$ is positive. In this case, clock period should satisfy

$$T_{clock} \ge T_{skew,12} + t_{c2q} + t_{com} + t_{setup}.$$
(2.3)

According to (2.3), a positive clock skew reduces the effective clock period and



Figure 2.10: Flip-flop min delay constraint with zero clock skew.

increases the sequencing overhead. Alternatively, a negative clock skew provides additional time for computations. Therefore, a negative clock skew can improve max delay timing constraints.

Ideally, sequencing elements can be placed back-to-back without any combinational logic. However, if the hold time is large and the clock-to-Q delay is small, the capture element can incorrectly latch data on the same clock edge. This situation is referred to as a race condition, hold time failure or min delay failure. This failure can only be fixed by slowing down the data signal. Therefore, min delay violations can only be fixed by redesigning the circuit.

A min delay timing constraint on the data path from R1 to R2 is shown in Fig. 2.10, assuming zero clock skew. As the rising edge of clock signal CK1 triggers R1, the data at D1 is latched in. It propagates through combinational logic circuit and must not reach D2 until at least the hold time after the same clock edge,



Figure 2.11: Flip-flop min delay constraint with negative clock skew.

otherwise the early arrival of the data may corrupt the contents of R2. This implies

$$t_{c2q} + t_{com} \ge t_{hold},\tag{2.4}$$

where t_{c2q} , t_{com} and t_{hold} represent clock-to-Q delay, propagation delay of combinational logic circuit and hold time, respectively.

A min delay timing constraint with nonzero skew case is shown in Fig. 2.11. Clock signal arrives R1 earlier than R2. Therefore, skew is negative. To ensure the correct functionality, the following inequality should be satisfied

$$T_{skew,12} + t_{c2q} + t_{com} \ge t_{hold}.$$
 (2.5)

According to (2.5), a negative skew can offset the propagation delay of combinational logic, making the circuit more sensitive to hold time violations. Alternatively, a positive skew decreases the effective hold time, which lowers the chances of a hold time failure.

2.1.4 Clock Tree Synthesis (CTS)

The process of a clock tree synthesis consists of two steps [41,42]: first step is to determine a set of clock arrival times for each register within the circuit, which satisfies all of the synchronous timing constraints mentioned in Section 2.1.3. This step is typically referred to as clock skew scheduling which is discussed in detail in Chapter 5. The second step is the physical layout of the clock network that implements the feasible clock schedule from step one, which is referred to as clock routing.

A set of feasible clock arrival time for each register within the clock network is generated after clock skew scheduling. The clock tree routing process constructs a tree topology with minimum wiring cost, while implementing the specified skew schedule generated in the previous step. Typically, a general clock routing algorithm includes two steps. First step is to generate an abstract topology and second step is to embed the abstract topology while satisfying the constraints. Various clock routing algorithms were proposed in the literature, which can be categorized into three domains: (1) zero-skew clock routing, (2) bounded skew routing, and (3) useful-skew clock routing. In [43-45], the proposed algorithms are based on zero-skew clock routing while minimizing wiring cost as an optimization objective. The bounded skew routing algorithms were proposed in [46, 47], which are an extension of the common zero-skew: deferred merge embedding (DME) algorithm. In [48, 48, 49], useful-skew based clock routing algorithms were developed while minimizing the wire cost and overall clock buffer size. In Chapter 6, a slew-driven clock tree synthesis methodology is proposed to simultaneously satisfy the clock skew and slew while constructing the clock tree bottom-up. Contrary to the delay/skew driven methodologies, the proposed approach prioritizes slew and reduces



Figure 2.12: An abstract tree.

the overall clock tree power.

An abstract topology G of a clock tree is a binary tree such that all of the sinks are the leaf nodes of the binary tree. A nonleaf node is either the clock source or internal nodes. Each internal node of G has two children, which are normally named as "left child" and "right child". The clock source node possibly has only one child. The root of the abstract tree is denoted as s0, which is also the source driver. Each non-root node v is connected to its parent, denoted as p(v), by an edge e_v . The clock signal from the source propagates through parent nodes to children nodes. An abstract tree topology with three leaves s1, s2 and s3 is shown in Fig. 2.12.

The embedding of an abstract topology *G* to form an interconnect tree *T* involves the mapping of each internal node $v \in G$ to a location (x_v, y_v) in the floorplan, where x_v and y_v are the *x* and *y* coordinates, and replacing each edge $e \in G$ by

a rectilinear edge or path [41]. Note that most of the clock routing algorithms only map the internal nodes in an abstract topology to physical locations on a floorplan and do not actually route the interconnects, which can be accomplished by a router tool. The wiring cost to route a tree T is the sum of all of its edges.

2.2 Existing Works on Low Voltage Clocking

Pangjun and Sapatnekar developed a low voltage/swing clock network by utilizing level converters [24]. Both single voltage and dual voltage converters were considered. A theoretical framework was proposed to appropriately position the low-to-high level converters throughout the clock tree. For example, two sinks that are physically close share a single converter to minimize the overall overhead. The primary limitation of this approach is the conversion of the clock signal back to full swing at the last stage of the clock tree. This practice significantly reduces the power savings due to high switching capacitance at the sink nodes. In addition, the slew constraint is considered as a secondary design objective after the merging points are determined during clock tree synthesis. As observed in this research, this approach generates a non-optimal low swing clock tree with reduced power savings.

Asgari and Sachdev proposed a low swing clock network design methodology using a single supply voltage [25]. In this approach, single voltage buffers are used to adjust the clock swing throughout the clock network. Similar to [24], clock voltage is restored to full swing at the last stage, thereby significantly reducing the overall power savings. In addition, the clock swing is tuned by relying on the delay of an inverter chain. Thus, the clock swing is highly dependent upon the output load capacitance, limiting the proposed approach to only highly symmetric clock networks such as H-trees.

More recently, low voltage clock networks have been investigated for nearthreshold systems that aim enhanced energy efficiency. In [28], Seok *et al.* investigated the skew characteristics of various clock networks operating at low voltages. The primary emphasis is on symmetric networks such as H-trees. Automated clock tree synthesis algorithms were not considered. In [27, 29], Zhao *et al.* proposed a deferred-merge embedding (DME) based clock tree synthesis method for low voltage clock networks with emphasis on clock slew. The proposed technique relies on a computationally expensive procedure of storing multiple solutions in a bottom-up fashion, followed by selecting an optimum solution for each node in a top-down fashion. Clock frequencies of less than 10 MHz are considered, limiting the proposed approach to only ultra low power systems where performance requirements are low.

2.3 Primary Challenges in Developing a Low Voltage Clock Network

Several challenges exist in the application of low voltage clocking to industrial circuits with heavily gated clock networks. These challenges and proposed solutions are summarized here.
2.3.1 Low Swing Operation at the Sinks: New Flip-Flop Cell

Traditional low swing clocking methodologies restore clock signals back to full swing at the sinks since conventional flip-flops cannot be reliably used with a low swing clock signal. A low swing clock signal either causes significant contention/short circuit current (thereby significantly increasing the power consumption) and/or increase clock-to-Q delay (thereby possibly violating the timing constraints) [50–52]. An important disadvantage of restoring back to full swing signal is a significant reduction in power savings since the last stage of a clock network consumes large power due to high capacitance. Thus, to maximize power savings, a novel flip-flop cell is developed to enable low swing operation at the sinks while still maintaining a full swing data signal, as further discussed in Chapter 3.

2.3.2 Satisfy Skew and Slew Constraints: Novel CTS and Level Shifter

At scaled supply voltages (as required for low swing operation), clock insertion delay increases, which in turn increases clock skew under variations. Furthermore, the drive ability of the clock buffers is degraded, which significantly increases clock slew. Satisfying the slew constraint at low swing operation therefore becomes highly challenging [53, 54]. A larger number of clock buffers is typically required which reduces the power savings. Research results demonstrate that an optimum voltage swing level exists beyond which low swing clocking increases overall power due to excessive buffering (assuming tight slew constraints) [55, 56]. A slew driven CTS algorithm is developed to satisfy the skew, slew constraints as in full swing operation, while also reducing clock network power consumption, as described in Chapter 6. A novel level-up shifter with dual supply voltage is also proposed for selective low swing clocking, as described in Chapter 4. The proposed level-up shifter enables a clock tree with both nominal and low voltages to simultaneously satisfy performance requirements and reduce power consumption.

2.3.3 Degraded Enable Path Timing: Exploit Useful Skew



Figure 2.13: A simplified gated clock network consisting of five sinks, an integrated clock gating (ICG) cell, and an *Enable* path.

Practical clock networks are heavily clock gated to reduce the switching activity factor of a clock signal, thereby reducing dynamic power. A common practice is to use integrated clock gating (ICG) cells that consist of a sequential element to prevent glitches in the gated clock signal, as shown in Fig. 2.13. An ICG cell has two input pins (clock and Enable signals) and an output pin (gated clock signal). The proposed low swing methodology should efficiently consider gated trees. Despite full swing operation of the data signals, it has been observed that low swing gated clock trees may violate timing constraints within an *Enable* path. Specifically, in

low swing operation, the delay between an ICG and flip-flops (gated by this ICG) increases. Thus, the timing of the *Enable* path suffers due to skew between the launching flip-flop and the capturing latch (within the ICG) [57,58]. Useful skew is exploited for gated low swing clock trees to alleviate this issue, as further discussed in Chapter 5.

Chapter 3

Flip-Flop Design to Facilitate Low Swing Operation

Existing works on low swing/voltage clock networks are effective primarily for low power applications that do not demand high performance. Achieving a reliable low swing clock network without sacrificing performance is challenging. The interface between a low swing clock signal and flip-flop may increase clock-to-Q delay, thereby reducing the timing slack within the data paths while also increasing power consumption. To alleviate this issue, a common approach is to restore full swing operation before the clock signal reaches flip-flops [24, 25]. This approach significantly reduces power savings since the last stage of a clock network has high switching capacitance. In this chapter, a novel D-type flip-flop design to facilitate low swing operation is explored. The proposed DFF can work reliably with a low swing clock signal while keeping the data signal as full swing, *i.e.*, not sacrificing the circuit performance. The rest of this chapter is organized as follows. Effect of low swing operation on flip-flop is investigated in Section 3.1. Existing works on low swing flip-flops are discussed in Section 3.2. The proposed topology is described in Section 3.3. Simulation results in 45 nm and 32 nm technology nodes are provided in Section 3.4. Finally, the proposed design is summarized in Section 3.5.

3.1 Effect of Low Swing Operation on Flip-Flop

As emphasized in Section 2.2, it is critical to have low swing operation at the DFF clock pins to maximize power savings. A conventional DFF cell designed for full swing operation, however, cannot be used when the clock voltage swing is reduced due to degradations in reliability and power consumption, as described in the following subsections.

3.1.1 Reliability

In a typical DFF cell, clock signals drive both NMOS and PMOS transistors (as in transmission gated based and tri-state inverter based DFFs). If the same DFF topology is used with a low swing clock signal (whereas the data signal is still at full swing to maintain performance), the PMOS transistors driven by the clock signal fail to completely turn off when the clock signal is high. For example, consider a 45 nm technology with a nominal V_{DD} of 1 V. If the clock swing is reduced to $0.7 \times V_{DD}$, the gate-to-source voltage of the PMOS transistors becomes -0.3 V since the data signal is at full swing and the inverters within the flip-flop are connected to nominal (full swing) V_{DD} . Since -0.3 V is sufficiently close to the threshold voltage of PMOS transistors in this technology, this behavior significantly affects the operation reliability of a traditional DFF cell driven by a low swing clock signal.



Figure 3.1: A typical transmission gate based D flip-flop topology driven by a low swing clock signal.

As an example, consider a rising-edge triggered master-slave flip-flop. When the clock signal is high, the master latch should be turned off. However, due to low swing clock signal, the transmission gate (or tri-state inverter) within the master latch cannot completely turn off. If the data signal is in a different state than the stored data within the master latch, a race condition occurs which can possibly produce a metastable state.

To better illustrate the unreliability of conventional DFF cells operating with a low swing clock signal, a traditional transmission gate based D flip-flop, as shown in Fig. 3.1, is simulated with a 45 nm technology node when the clock swing is 0.7 V. Note that the clock signal and inverted clock signal are internally generated by using two inverters. This circuit is referred to as the clock sub-circuit, as also depicted in Fig. 3.1. Note that the inverters within the clock sub-circuit are connected to a low supply voltage to provide low swing clock signals. Since the PMOS transistors driven by the clock signals are not completely turned off, internal nodes experience

a glitch as high as 400 mV. Furthermore, in the slow corner, the DFF cell fails to correctly latch the data signal. Thus, a new topology is required that can reliably operate with a low swing clock signal and a full swing data signal.

Note that an alternative solution is to integrate a level shifter within the DFF cell to restore a full swing clock signal [59]. Thus, the clock signal is restored to full swing operation before reaching PMOS transistors. This approach is similar to existing level shifting DFF cells for dual voltage systems [60], but the level of the clock signal is shifted rather than the data signal. This approach, however, significantly increases the overall power consumption of the DFF cell due to the integrated level shifter. Thus, the power saved at the last stage of the clock network is lost within the DFFs, making this approach impractical for the primary objective of this work.

3.1.2 Power Consumption

The reliability issue described in the previous subsection can be fixed by connecting the inverters within the clock sub-circuit of a conventional DFF to the nominal V_{DD} , producing a single voltage flip-flop driven by a low swing clock signal. In this case, these inverters also function as single voltage, low-to-high level shifters and the transmission gates receive full swing clock signals. The primary limitation of this approach is an unavoidable increase in power consumption due to significant static current drawn by the inverters within the clock sub-circuit. To better illustrate this behavior, a conventional DFF is simulated when a low swing clock signal is applied to the clock pin while the clock sub-circuit is connected to a nominal V_{DD} . The overall power consumption is shown in Fig. 3.2 as a function of clock swing for both 45 nm and 32 nm technologies. As shown in this figure, DFF power increases



Figure 3.2: Increase in power consumption when a conventional DFF is driven with a low swing clock signal while the clock sub-circuit is connected to a nominal V_{DD} .

by approximately 48% and 23% when the clock swing is reduced to $0.6 \times V_{DD}$ in, respectively, 45 nm and 32 nm technologies.

Thus, a conventional flip-flop designed for a full swing clock signal suffers from a prohibiting trade-off between reliability and power consumption. The reliability issue may cause the flip-flop to latch a wrong data due to large spikes, which is exacerbated in corner cases. Alternatively, the increase in power consumption is not tolerable since it conflicts with the primary purpose of this work.

3.2 Existing Low Swing Flip-Flops

Existing flip-flop topologies developed to operate with a low swing clock signal are summarized in this action. The strengths and weaknesses of each topology are discussed.





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A flip-flop topology for a low swing clock signal based on clocked CMOS method (C^2MOS) and sense amplifier (SA) has been proposed in [1], as illustrated in Fig. 3.3(a). This circuit, referred to as $L-C^2MOS-SA$, reduces the chargedischarge capacitance and implements the conditional pre-charge and discharge technique to achieve low power consumption. The circuit is area efficient and a considerable reduction in leakage current is also obtained with this topology. The original version of this topology utilizes diode-connected PMOS transistors within the clock sub-circuit to reduce voltage swing, as depicted in Fig. 3.3(a). Diodeconnected PMOS transistors, however, significantly degrade clock slew due to reduced supply voltage in stacked PMOS transistors, making this topology impractical for industrial circuits. This issue is exacerbated in the slow corner operation. Thus, to achieve a fair comparison, this topology is modified in this work where the clock sub-circuit has a second power supply voltage for low swing rather than having diode-connected PMOS transistors. This modified version is referred to as L-C²MOS-SA-2. Also note that this topology requires a full swing clock signal at the slave stage, which defies our primary objective of having only a low swing clock signal throughout the entire clock network.

Another flip-flop topology has been proposed in [2] for low swing operation. This topology, referred to as reduced clock swing flipflop (RCSFF), is depicted in Fig. 3.3(b). As shown in this figure, this design utilizes an additional low supply voltage within the clock sub-circuit to provide low swing clock signal, similar to the proposed topology in this research. However, in [2], the low swing clock signal is used to drive PMOS transistors that are connected to a higher (full) supply voltage. As mentioned earlier, these transistors cannot completely turn off, producing functionality and reliability issues in addition to significantly increasing both short circuit and leakage current. To alleviate this issue, authors have utilized the well known bulk biasing technique. Specifically, the bulk nodes are connected to a separate well biased at a greater voltage, thereby increasing the threshold voltage of these PMOS transistors. An additional well, however, not only increases the physical area and complexity of the design, but also requires a triple-well process that is not common in standard digital CMOS technologies. Furthermore, at the corner cases, this issue is exacerbated despite the use of well biasing.

The NAND-type keeper flip-flop topology proposed in [3], referred to as ND-KFF, is illustrated in Fig. 3.3(c). As opposed to the previous topology, this circuit does not require a separate well at the expense of excessive leakage current that flows through the transistors P2, N1-N3 when node X is at logic low. Furthermore, a contention occurs at node X since the level-keeping transistors, i.e., P2, N4, N5 and I1-I2 have a race condition when node X transitions from logic low to logic high, thereby increasing the transition time and clock-to-Q delay of the output. This issue is exacerbated during the worst-case delay analysis of the circuit, which can be partially controlled by carefully sizing the transistors.

In [4], authors have proposed a contention reduced flip-flop referred to as CRFF and is depicted in Fig. 3.3(d). This circuit utilizes a pulsed clock signal to provide a short transparency window during which the output is discharged through the NMOS transistors N1-N4. During this transparency window, the clocked transistors P5 and P6 disconnect the latch (I1-I2), thereby reducing contention current. Transistors P1 and P2 are controlled by input D through P3 and P4 which further reduces the contention current. However, low swing clock signal is used to drive PMOS transistors P5 and P6, thereby suffering from the aforementioned issues of functionality and reliability.

3.3 Proposed D-Flip-Flop Topology for Low Swing Clocking

The proposed DFF topology, depicted in Fig. 3.4(a), is based on the most commonly used, static D flip-flop shown in Fig. 3.1. Rather than using transmission gates, however, pass gates with NMOS transistors (N1, N2, N5, and N6) are utilized as the switches in both master and slave latches. Thus, when the low swing clock signal is at logic high, N1 and N6 can completely turn off. Pass gates, however, cannot transfer a full voltage to the output. This issue is critical since the incoming data signal operates at full swing. Thus, node A cannot reach a full V_{DD} , thereby increasing the short-circuit and leakage current in the following stages in addition to increasing the clock-to-Q delay. Furthermore, pass transistors are known to be less robust to process variations. To alleviate these issues, a pull-up network consisting of two PMOS transistors is added to both master and slave latches (P1 to P4). When the master node M transitions to logic low, P1 turns on. If the data signal is also at logic low, then node A is pulled to full V_{DD} through P1 and P2. Note that P2 (in the master latch) and P4 (in the slave latch) are added to prevent contention current (and therefore reduce power consumption) when the data signal is at logic high and clock signal is at logic low. In this situation, N1 is on and node A is discharged through N1 and the inverter. If P2 does not exist, a race condition occurs at node A since N1 should be stronger than P1, which pulls node Y to full V_{DD} . Finally, a pull-down logic is added to both master and slave latches to enhance clock-to-Q delay (N3, N4, N7, and N8). Specifically, when data and clock signals are at logic low, the pull-down logic is active and pulls the master node M to ground, triggering P1. Thus, node A quickly reaches full V_{DD} . Note that the master node does not need



(b)

Figure 3.4: Proposed DFF topology that can reliably work with a low swing clock signal whereas the data and output signals are at full swing, (a) schematic, (b) layout in the 45 nm technology.

to wait for node A to rise through a weak pass transistor and activate the inverter. Instead, the pull-down logic completes this transition relatively faster. Also note that the clock sub-circuit is identical to the sub-circuit shown in Fig. 3.1. Layout of the proposed DFF topology in a 45 nm technology is depicted in Fig. 3.4(b).

3.4 Simulation Results

The proposed low swing flip-flop is compared with the conventional full swing flip-flop on power and clock-to-Q delay as clock swing varies in Section 3.4.1. A comparative analysis with existing works including robustness of each topology to PVT variations is presented in Section 3.4.2.

3.4.1 Comparison with Conventional Full Swing Flip-flop



Figure 3.5: Correct functionality of the proposed low swing DFF cell in 32 nm technology: (a) latching logic-low, (b) latching logic-high.

The proposed low swing DFF topology is designed in both 45 nm and 32 nm technologies. To illustrate proper functionality, full swing data, low swing clock, and full swing output (Q) signals are plotted in Fig. 3.5 for the 32 nm technology

while driving a 5 fF load capacitance. As shown in this figure, the DFF cell can successfully latch both logic-low and logic-high full swing data signals after the rising edge of the low swing clock signal. Note that the output reaches nominal (full swing) V_{DD} and the DFF cell does not exhibit glitches in any of the internal nodes.



Figure 3.6: Power consumption comparison of the proposed low swing DFF cell (LSDFF) with the conventional full swing DFF cell (FSDFF): (a) 45 nm technology, (b) 32 nm technology.

To compare the proposed low swing DFF cell (LSDFF) with the conventional full swing DFF cell (FSDFF), power and clock-to-Q delay are analyzed as a function of clock swing for both 45 nm and 32 nm technologies. The overall power consumption is compared in Fig. 3.6. According to this figure, for both technologies, FSDFF consumes less power than LSDFF at relatively large clock swings. As the clock swing is reduced, however, LSDFF significantly outperforms FSDFF. The crossover voltage is approximately 0.85 V for 45 nm technology and 0.81 V for 32

nm technology. At a clock swing of 0.6 V, LSDFF consumes approximately 53% and 30% less power than FSDFF in, respectively, 45 nm and 32 nm technologies.



Figure 3.7: Clock-to-Q delay comparison of the proposed low swing DFF cell (LS-DFF) with the conventional full swing DFF cell (FSDFF): (a) 45 nm technology, (b) 32 nm technology.

The clock-to-Q delay of the LSDFF and FSDFF is compared as a function of clock swing in Fig. 3.7. According to this figure, for both technologies, LSDFF outperforms FSDFF in all clock swings except 0.6 V in 32 nm technology. The clock-to-Q delay of the LSDFF at this point is only 5 ps more than FSDFF. It is important to note that the LSDFF running at 0.65 V can achieve less or equal clock-to-Q delay than FSDFF running at full swing. This characteristic is highly important to maintain data path timing the same (or with more slack) when the conventional flip-flops are replaced with LSDFFs. The clock-to-Q delay in LSDFF is adjusted by sizing the last two inverter stages. Note that the clock pin capacitance remains the same as FSDFF, since the size of the first inverter within the clock subcircuit (see Fig. 3.1) is kept constant. Also note that, for a fair analysis, the size of the

transistors within the flip-flops remains the same at each clock voltage.

The timing constraint characterization of the LSDFF and FSDFF demonstrates that the proposed topology has comparable setup and hold times, as listed in Table 3.1. In particular, for hold time, LSDFF slightly outperforms FSDFF. This characteristic is important to ensure that no min-delay constraint violations are introduced in short data paths. Alternatively, for setup time, FSDFF slightly outperforms LSDFF. The difference, however, is sufficiently small as compared with the clock period in multigigahertz designs.

Topology		45 nm		32 nm	
		FSDFF	LSDFF	FSDFF	LSDFF
Setup time (ps)	Latch 1	11	23	4	18
	Latch 0	12	28	6	26
Hold time (ps)	Latch 1	-1	-15	-2	-15
	Latch 0	-7	-19	2	-7

Table 3.1: Setup and hold time simulation results of full swing DFF and the proposed low swing DFF at 45 and 32 nm technology nodes.

The proposed LSDFF has also been simulated at the slow and fast corners to evaluate the robustness of the topology to PVT variations. As listed in Table 3.2, at a clock swing of 0.7 V, the proposed topology achieves reliable operation and outperforms the conventional topology at each corner (nominal, slow, and fast).

Finally, the cell area consumed by the proposed and existing topologies is listed in Table 3.3. According to Table 3.3, LSDFF consumes 50% and 55% additional area for, respectively, 45- and 32-nm technologies. The effect of this increase in the overall die area, however, is expected to be below 10% considering the typical percentage of the flip-flops in a design.

Topology	45 nm		32 nm		
Topology	FSDFF	LSDFF	FSDFF	LSDFF	
Nominal corner (TT me	odel, 1.0V	and 1.05	V supply a	nd 25°C)	
Clock-to-Q delay (ps)	86.16	68.39	95.93	77.50	
Dynamic power (µW)	10.75	7.24	3.63	2.77	
Worst corner (SS model, 0.9V and 0.95V supply and 125°C)					
Clock-to-Q delay (ps)	183.95	180.44	181.86	175.19	
Dynamic power (μ W)	6.83	5.86	2.18	2.05	
Best corner (FF model, 1.1V and 1.15V supply and -40°C)					
Clock-to-Q delay (ps)	57.02	26.12	55.06	15.69	
Dynamic power (µW)	21.62	9.28	9.69	9.78	

Table 3.2: Corner simulation results of full swing DFF and the proposed low swing DFF at 45 and 32 nm technology nodes.

Topology		Area (μ m \times μ m)
45 nm	FSDFF	3.285×2.67=8.77
	LSDFF	4.93×2.67=13.16
32 nm	FSDFF	2.674×1.672=4.47
	LSDFF	4.166×1.672=6.96

Table 3.3: Layout areas of full swing DFF and the proposed low swing DFF at 45 and 32 nm technology nodes.

3.4.2 Comparison with Existing Low Swing Flip-flops

The proposed flip-flop topology and the previous circuits in existing work (L- C^2MOS -SA [1], L- C^2MOS -SA-2 [1], RCSFF [2], NDKFF [3], and CRFF [4]) are designed using a 45 nm technology with a nominal supply voltage of 1 V and all of the simulations are performed using Spectre [61]. The clock signal has a reduced swing of 0.7 V. The clock and data frequencies are, respectively, 1.5 GHz and 150 MHz. Each flip-flop drives an output load capacitance of 5 fF. To achieve a fair comparison, all of the flip-flops are sized to produce approximately equal clock-

to-Q delay. The simulations results including a comparative analysis with existing work are presented in Section 3.4.2.1. Robustness of each topology to process, voltage, and temperature variations is investigated in Section 3.4.2.2.

3.4.2.1 Comparative Analysis

The simulation results are listed in Table 3.4, comparing clock-to-Q delay, power consumption, power-delay product (PDP), leakage power, overall transistor size, and setup and hold times of all of the flip-flops. Note that the leakage power listed in this table is obtained by averaging the leakage power obtained from four possible static combinations of the data and clock signals.

As listed in Table 3.4, the proposed topology achieves, on average, 38.1% and 44.4% reduction in, respectively, dynamic power and power-delay product while exhibiting similar clock-to-Q delay. L-C²MOS-SA [1] achieves the least leakage power that is approximately 45% less than the proposed topology. L-C²MOS-SA [1], however, exhibits degraded behavior at the worst-case corners, as described in Section 3.4.2.2. The proposed topology exhibits the second lowest leakage power, achieving significant reduction, particularly as compared to NDKFF [3] and CRFF [4]. Overall transistor width of the proposed topology is less than the other topologies except L-C²MOS-SA [1]. The setup-hold time characterization of each topology is also performed, as listed in the last two columns [62]. Similar to some other topologies, the proposed flip-flop exhibits a negative setup time.

The effect of clock swing voltage level on clock-to-Q delay and power consumption is also investigated for each flip-flop, as depicted in Fig. 3.8.

According to Fig. 3.8(a), clock-to-Q delay increases as the clock swing is reduced in each topology. For L-C²MOS-SA [1], NDKFF [3], and CRFF [4], clock

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Flip-flop	Clock-to-Q	Overall	PDP	Leakage	Overall t	transistor	Setup	Hold
topology	delay	power	(fW.s)	power	wi	dth	time	time
	(sd)	(Mn)		(NN)	NMOS	PMOS	(sd)	(sd)
					(uu)	(uu)		
L-C ² MOS-SA [1]	69.7	8.0	0.56	37.2	2395	2950	27.9	0.9
L-C ² MOS-SA-2 [1]	71.3	9.3	0.67	34.5	4195	3550	17.5	-9.2
RCSFF [2]	70.6	17.2	1.22	82.0	6840	5500	-26.9	42.6
NDKFF [3]	69.4	12.0	0.83	196.6	5050	3900	-6.0	-62.7
CRFF [4]	70.3	10.5	0.74	201.5	4650	5300	-20.2	92.9
Proposed LSDFF	64.1	6.6	0.42	68.1	2650	3450	-1.7	17.8



Figure 3.8: Effect of clock swing voltage level on clock-to-Q delay and power consumption for each flip-flop topology: (a) Clock-to-Q delay vs. clock voltage swing, (b) power consumption vs. clock voltage swing.

swing cannot be reduced below 0.6 V since these circuits fail to latch the input data at clock swings lower than 0.6 V. Note that the clock-to-Q delay is highly sensitive to voltage swing for NDKFF [3]. The proposed topology can reliably latch the input data for a clock swing as low as 0.5 V (half V_{DD}). Furthermore, the proposed topology exhibits relatively low sensitivity to voltage swing. RCSFF [2] is the only topology that can work with a clock swing as low as 0.4 V. However, the clock-to-Q delay significantly increases below 0.5 V, making this operating point impractical. Furthermore, RCSFF [2] consumes significantly more power than the proposed topology, as listed in Table 3.4.

The dependence of power consumption on clock voltage swing is shown in Fig. 3.8(b). According to this figure, the proposed topology exhibits the lowest power consumption at each clock swing voltage. Note that from 0.7 V to 0.6 V, the overall power is slightly reduced whereas from 0.6 V to 0.5 V, there is a slight increase. The overall effect of clock swing on power depends upon two factors: 1)

Flip-flop topology	CLK-to-Q delay (ps) at SS-0.9V-165°C	Overall transient power (µW) at FF-1.1V	Leakage power (µW) at FF-1.1V-165°C
L-C ² MOS-SA [1]	Failure	10.8 (T=165°C)	0.6
L-C ² MOS-SA-2 [1]	178.8	11.3 (T=165°C)	0.6
RCSFF [2]	Failure	21.5 (T=-40°C)	1.5
NDKFF [3]	210.0	17.2 (T=165°C)	2.5
CRFF [4]	175.7	17.7 (T=165°C)	3.8
This work	150.8	8.9 (T=-40°C)	1.1

Table 3.5: Comparison of the proposed topology with existing work under worstcase operating conditions for clock-to-Q delay, overall transient power, and leakage power. FF and SS correspond, respectively, to fast and slow models for both NMOS and PMOS transistors.

partial reduction in power since the clock sub-circuit consumes less power with a lower swing, 2) partial increase in power due to a greater contention current with a lower clock swing. If the first factor outweighs the second factor, overall power is reduced as the clock swing is reduced. Note that CRFF [4] is the only topology where power consumption significantly increases with a lower clock swing, indicating the dominance of the second factor.

3.4.2.2 Robustness to Variations

A critical challenge in nanoscale ICs is the variations incurred during fabrication and fluctuations in operating voltage and temperature. The behavior of a circuit to these variations is important to evaluate the overall robustness. To investigate this issue, each flip-flop topology is simulated in the worst-case corner for delay, transient power, and leakage power. The results are listed in Table 3.5. Note that L-C²MOS-SA [1] and RCSFF [2] fail to latch the input data at the worst-case corner for delay, determined by the slow process models for both NMOS and PMOS transistors, 0.9 V V_{DD} (90% of the nominal V_{DD}) and 165°C temperature.

The proposed topology exhibits the lowest clock-to-Q delay (approximately 20% lower, on average) in the worst-case corner even though each topology exhibits similar delays in the nominal case (see Table 3.4). This trend demonstrates that the clock-to-Q delay of the proposed topology exhibits the least sensitivity to process and environmental variations.

Similar to the nominal case, the proposed topology consumes the least transient power in the worst-case, as determined by the fast process models for both NMOS and PMOS transistors and 1.1 V V_{DD} (110% of the nominal V_{DD}). Note that the temperature that corresponds to the worst-case corner for overall power depends upon the topology due to inverted temperature dependence [63].

Specifically, in RCSFF [2] and the proposed topologies, the worst-case transient power occurs at the lowest temperature whereas the other topologies consume the largest power at the highest temperature. Note that inverted temperature dependence also applies to the worst-case delay analysis and therefore each topology is simulated with both the lowest and highest temperatures. However, largest clockto-Q delay occurs at the highest temperature in each topology, as shown by the second column in Table 3.4. Finally, the worst-case leakage power, determined by the fast process models, 1.1 V V_{DD} , and highest temperature, is provided in the last column. The trend is similar to the nominal results where the proposed topology consumes the second least leakage power, after L-C²MOS-SA [1].

The variation analysis provided in this section demonstrates that the proposed topology can reliably operate at the worst-case delay and power corners, unlike some of the existing topologies that fail at the worst-case delay corner. Furthermore, the proposed topology consumes the least worst-case power consumption and exhibits the least sensitivity to worst-case delay corner.

3.5 Summary

In this chapter, a D-type static flip-flop is proposed to facilitate low swing operation. It can reliably operate with a low swing clock signal, thereby enabling low swing operation throughout the entire clock network. Thus, power savings are maximized. Simulation results on power-delay product, corner performance, setup/hold time demonstrate the superiority of the proposed DFF at each clock swing for both 45 nm and 32 nm technologies.

Chapter 4

Level Shifter for Selective Low Swing Clocking

In clock trees with highly aggressive design constraints (such as small skew and slew), it may not be practical to lower the clock voltage of the entire clock tree. Selective low voltage clocking has been considered for such situations where part of the clock tree operates at a reduced voltage (to save power) and the rest of the tree operates at nominal voltage to satisfy the performance constraints. Thus, a low overhead level shifter is required to restore clock voltage level. In Fig. 4.1, sink 2 and 3 are restored to full swing operation through a level-up shifter to satisfy their timing constraint, while the rest of the sinks are still in low swing operation to achieve power savings.

Existing level shifters can be categorized under two primary classes: 1) shifters based on conventional, cross-coupled topology with differential output [64–67], 2) shifters based on bootstrapping [68, 69]. Shifters in the first group enhance the



Figure 4.1: Selective low swing clocking.

delay of the level shifting by exploiting cross-coupled PMOS transistors whereas shifters in the second group enhance the power consumption by reducing the swing at the internal voltage nodes. In some applications where sub-threshold circuits are interfaced with super-threshold operation, wide range level shifters are required, as proposed in [65, 70, 71]. Level shifters with a single supply voltage have also been proposed [72, 73]. However, shifting voltage swing with a single supply voltage typically produces large leakage current and long signal transition times.

A conventional buffer consisting of two inverters powered by the lower supply voltage V_{ddL} can reliably function as a level-down shifter since there is no short circuit or leakage issue [24]. A conventional buffer, however, cannot reliably function as a level-up shifter since the incoming signal with a lower supply voltage drives inverters powered with a higher supply voltage. This situation causes unreasonably high short circuit and leakage current that is not tolerable in most of the

applications. For example, in 45 nm technology, if a conventional buffer is used as a level-up shifter, short circuit current is approximately 31% of the overall power consumption while leakage current is in the range of microamps.

In this chapter, a level-up shifter with dual supply voltage is proposed to enable selective low swing clocking. It reduces the transient power of conventional cross-coupled topology while consuming significantly less area as compared to bootstrapping technique. A relatively fast response is also achieved. The rest of this chapter is organized as follows. The traditional cross-coupled level shifter and bootstrapping techniques are summarized in Section 4.1 and Section 4.2, respectively. The proposed level shifter is described in Section 4.3. Simulation results and related discussion are presented in Section 4.4. Finally, the chapter is concluded in Section 4.5.

4.1 Cross-Coupled Topology

Conventional level shifter using cross-coupled PMOS transistors is depicted in Fig. 4.2(a). As shown in this figure, the incoming low voltage signal is inverted using an inverter connected to a low voltage domain, V_{ddL} . Cross-coupled PMOS transistors P1 and P2 are used to pull output to the high voltage, V_{ddH} . Leakage issue of the conventional buffer is alleviated since P1 and P2 are not driven by the incoming signal. However, this topology exhibits relatively high short circuit current during transition (either through P1 and N1 or through P2 and N2) even when the input transitions are fast.



Figure 4.2: Primary existing level shifters: (a) conventional cross-coupled topology, (b) bootstrapping technique.

4.2 Bootstrapping Technique

Bootstrapping technique, as depicted in Fig. 4.2(b), has been proposed to reduce the transient power during level shifting. Voltage swing at specific nodes is reduced, thereby saving power, particularly when driving large capacitive loads [69]. In Fig. 4.2(b), two boot capacitors C_{boot1} and C_{boot2} replace NMOS transistors to maintain the voltage difference at the gate terminals of P2 and N2. Thus, the pulldown NMOS N2 at output stage is driven between 0 and V_{ddL} whereas the pull-up PMOS is driven between $V_{ddH} - V_{ddL}$ and V_{ddH} . Bootstrapping technique achieves lower power at the expense of significant increase in physical area due to the relatively large boot capacitors, determined by

$$C_{boot1} = C_A \cdot \frac{2 \cdot V_{diode}}{V_{ddL} - 2 \cdot V_{diode}},\tag{4.1}$$

where C_A is total capacitance at node A to ground, excluding C_{boot1} . V_{diode} is the voltage drop across a single diode, similar to D0 in [68]. When V_{ddL} is sufficiently close to $2 \cdot V_{diode}$, boot capacitor becomes considerably large. In [69], cross-coupled load is divided into half and only one boot capacitor is required, partially reducing the overall area requirement.

4.3 Proposed Level Shifter for Selective Low Swing Clocking

The proposed level-up shifter schematic and physical layout are illustrated in Fig. 4.3(a) and Fig. 4.3(b). The proposed design is based on a traditional buffer with certain modifications to minimize short-circuit current, reduce delay while minimizing the overall number of transistors. Since an input signal at the V_{ddL} level cannot completely turn off PMOS transistors, an inverter is designed with two NMOS transistors (N1 and N2) where N2 is driven by inverted input signal. When input signal is at logic low, N1 is off and N2 is on. Node A is at $V_{ddH} - V_{th}$ since N2 cannot pass a full VDD. To compensate for the threshold voltage drop, two keeper PMOS transistors, P1 and P2, are added. When output node goes low, P2 is on.



Figure 4.3: Proposed level shifter (a) schematic, (b) physical layout.

Since input signal is also at logic low, node A is pulled to VDDH. Note that P1 is added to prevent short-circuit current when node A is being discharged through N1. A pull down NMOS transistor, N5, is added to reduce the delay when the output is having a high-to-low transition. If the input signal is at logic high, N1 is on, N2 is off. Node A is discharged through N1. Since P1 is off, no short-circuit current exists. As node A is discharged, output rises to VDDH through P4. The input and



Figure 4.4: Input and output waveforms of the proposed level shifter.

output waveforms of the proposed level shifter are illustrated in Fig. 4.4 where the low voltage domain is 0.7 V and high voltage domain is 1 V.

The signal switches at 1 GHz with 100 ps transition time and level shifter drives an output capacitance of 5 fF in a 45 nm technology. The proposed level shifter can work with input voltage domains as low as 0.45 V, as further described in the following section.

4.4 Simulation Results

Extracted simulations of four level shifters are performed:

- Traditional buffer consisting of two inverters
- Conventional cross-coupled topology (Fig. 4.2(a))
- Bootstrapping level shifter (Fig. 4.2(b))
- Proposed level shifter (Fig. 4.3(a))

Note that each level shifter is designed and extracted using a 45 nm technology. Extracted simulations are achieved at 1 GHz with 100 ps transition times while driving an output load of 5 fF capacitor. Low and high VDD levels are, respectively, 0.7 V and 1 V. Also note that the traditional buffer is included in the comparison only as a reference for delay and transient power. In practice, this topology is not suitable as a level shifter due to unreasonably high leakage and short circuit current, as mentioned before.

The extracted simulation results are presented in four parts: power-delay product for each level shifter is described in Section 4.4.1. Worst-case corner simulation results for delay, dynamic power, and leakage power are provided in Section 4.4.2. The dependence of each topology on input swing is analyzed in Section 4.4.3. Finally, the physical area consumed by each circuit is discussed in Section 4.4.4.

4.4.1 **Power-Delay Product**

The power-delay product for each level shifter is obtained as a function of scale factor, as shown in Fig. 4.5. The scale factor is the sizing factor for those transistors that affect the delay of the circuit in each level shifter. As shown in this figure, upsizing the critical transistors initially enhances the power-delay product, eventually reaching a minimum value. However, if the transistors are up-sized further, power-delay product starts to increase. Thus, by obtaining the power-delay product curves as a function of scale factor, each topology can be compared at the corresponding optimum design point where power-delay product is minimized. Note that when the scale factor is equal to 1, each topology exhibits approximately the same delay of 50 ps. According to Fig. 4.5, bootstrapping technique achieves the least power-delay product (excluding traditional buffer) that is 22% less than the proposed topology.



Figure 4.5: Power-delay product as a function of scale factor for each topology: (a) cross-coupled, (b) bootstrapped, (c) buffer, (d) proposed.

However, bootstrapping technique has significant area overhead, as quantified in Section 4.4.4. As compared to the cross-coupled level shifter, the proposed topology exhibits approximately 66% less power-delay product, which is a significant improvement over the most commonly used level shifter topology.

4.4.2 Nominal and Corner Simulation Results

Extracted simulation results at the nominal corner (typical models, 1 V supply and at 27° C) are listed in Table. 4.1.

The proposed level shifter achieves 43% reduction in transient power compared to cross-coupled topology while achieving almost the same delay. Leakage power is also reduced by 36%. As compared to bootstrapped topology, the proposed level

Topology	Tran. power (μ w)	Leakage (nw)	Delay (ps)	Slew (ps)
Cross-coupled	31.09	24.29	67.71	50.40
Bootstrapped	13.75	14.46	80.50	71.96
Buffer	8.43	850.62	56.29	50.13
Proposed	17.73	15.53	69.21	60.82

Table 4.1: Extracted results at nominal corner.

Topology	Transient power (μ w)	Average delay (ps)	Average slew (ps)			
Worst corner for delay						
Cross-coupled	23.77	139.18	138.13			
Bootstrapped	10.78	199.12	257.74			
Buffer	6.10	128.85	126.11			
Proposed	14.14	151.26	167.01			
Worst corner for transient power						
Cross-coupled	40.88	44.24	31.06			
Bootstrapped	17.15	47.24	34.90			
Buffer	14.22	37.34	32.12			
Proposed	22.73	42.85	35.69			

Table 4.2: Worst corner for delay (SS model, 0.9V supply and 165° C) and transient power (FF model, 1.1V supply and -40°C)

shifter achieves 14% less delay, but 28% more transient power. Bootstrapped topology, however, has significant area overhead (see Section 4.4.4). Output slew of each topology is comparable with a noticeable increase for the bootstrapped topology.

All of the topologies are analyzed at the worst-case corner for delay (slow models, 0.9 V, and 165°C), transient power (fast models, 1.1 V, and -40°C), and leakage power (fast models, 1.1 V, and 165°C). The results are listed, respectively, in Tables 4.2 and 4.3.

The proposed topology exhibits 24% less delay and 44% lower transient power at the worst corner as compared to bootstrapped and cross-coupled topologies, re-

Topology	Input @ V_{ddL} (nw)	Input @ gnd (nw)	Average (nw)
Cross-coupled	349.53	338.35	343.94
Bootstrapped	198.50	352.73	275.62
Buffer	4367.20	76.42	2221.81
Proposed	248.37	195.42	221.90

Table 4.3: Worst corner for leakage (FF model, 1.1V supply and 165°C)

spectively. Furthermore, the proposed level shifter achieves approximately 20% and 36% less leakage power than, respectively, bootstrapped and cross-coupled topologies in the worst corner.

4.4.3 Dependence on Input Swing

The behavior of each topology to different levels of input voltage is investigated in this section. Transient power and delay are shown in Figs. 4.6(a) and 4.6(b) as a function of input swing (V_{ddL}). According to Fig. 4.6(a), bootstrapped topology achieves lower power for input voltage domains less than 0.88 V. Proposed topology achieves significantly less power than the cross-coupled topology, particularly at input voltage domains less than 0.65 V. According to Fig. 4.6(b), proposed topology outperforms both cross-coupled and bootstrapped topologies in delay as input swing is reduced.

4.4.4 Area Comparison

All of the topologies are laid out using a standard cell design methodology where the height is fixed at 1.25 μ m. The physical area consumed by the cross-coupled, bootstrapped, and proposed topologies, are, respectively, 3.1 μ m², 13.65 μ m², and 2.8 μ m². Proposed topology consumes 9.5% and 79.5% less area as com-



Figure 4.6: Dependence on input supply voltage: (a) power as a function of input supply voltage, (b) delay as a function of input supply voltage.

pared to cross-coupled and bootstrapping topologies, respectively.

4.5 Summary

A novel dual supply level-up shifter is proposed for selective low swing operation. The proposed topology achieves 43% less transient power and 36% less
leakage power than the most commonly used cross-coupled topology, while also consuming 9.5% less area. As compared to bootstrapping technique, proposed topology achieves 79.5% reduction in physical area. Corner simulations are also performed, demonstrating the superior performance of the proposed level shifter.

Chapter 5

Exploiting Useful Skew in Gated Low Voltage Clock Trees for High Performance

Existing works on low swing/voltage clocking do not consider the performance requirements of the IC. In practice, low swing clocking introduces two issues related to performance: 1) possible degradation in clock-to-Q delay of the flip-flops due to low swing clock signal, 2) timing degradation in the *Enable* paths of a gated clock network due to higher clock insertion delay. A possible solution to the first issue is to restore the full swing/voltage operation before the clock signal reaches flip-flops [24]. This approach reduces the power savings since the last stage of a clock network has high switching capacitance. In Chapter 3, a novel flip-flop topology has been proposed for low swing clock signals without any degradation in clock-to-Q delay, addressing issue one. A methodology based on useful skew is

proposed in this chapter to address issue two.

Clock gating [74, 75] is a standard method to reduce dynamic power by deactivating the clock signals of the idle flip-flops. Thus, proposed methods based on low voltage/swing clocking should be able to consider clock gating. A simplified gated clock network is shown in Fig. 2.13. The clock signal can be gated by an integrated clock gating (ICG) cell, depending upon the *Enable* signal. If the *Enable* signal is active, the output of the ICG cell (gated clock signal) does not switch even though the clock signal switches, thereby reducing dynamic power in certain clock nets. Unfortunately, a low voltage/swing clock signal degrades the timing of the *Enable* path even when the data signals are at nominal voltage, as further described in Section 5.1.3.

A useful skew approach is formulated in this chapter for gated clock networks operating at a reduced voltage. The methodology is evaluated on largest ISCAS'89 benchmark circuits, demonstrating that the useful skew can effectively fix timing violations (introduced due to low voltage/swing operation) within the *Enable* paths.

The rest of this chapter is organized as follows. Background on low swing operation and problem formulation are provided in Section 5.1. The proposed method is described in Section 5.2. Experimental results on several large ISCAS'89 benchmark circuits are presented in Section 5.3. The chapter is concluded in Section 5.4.

5.1 Background on Low Swing Operation and Problem Formulation

Historically, the clock skew is managed in three ways: i) zero skew, ii) bounded skew and iii) useful skew approaches, *i.e.*, clock skew scheduling. The zero skew and bounded skew approaches ensure that the clock arrival time of all of the sequential elements is either identical (for zero skew) or within a margin (for bounded skew). Alternatively, the useful skew approach considers clock skew scheduling where the skew of each sequential element that belongs to the same timing path is individually considered for timing optimization. In clock skew scheduling, the available timing slack at each sequential element is utilized to improve clock period of the IC. Specifically, slower data paths "borrow" time from faster data paths. Thus, skew scheduling exploits the mismatches in the timing characteristics of the data paths to decrease clock period.

Conventional clock skew scheduling techniques rely on linear programming (LP) with a minimum clock period objective [11, 76, 77] or a graph-based solution to utilize existing graph algorithms [78,79]. In [80], delay insertion methodology in clock skew scheduling is proposed. In [81], a linear programming approach is proposed to minimize the overall delay insertion while maintaining the minimum clock period. In order to mitigate the effect process variations on skew, multi-domain clock skew scheduling [82] is proposed. In [83, 84], two optimal algorithms are developed to implement a multi-domain clock skew scheduling.

Traditional clock skew scheduling is briefly summarized in Section 5.1.1. Unique challenges introduced due to clock gating are discussed in Section 5.1.2. *Enable* path timing in low swing operation is introduced in Section 5.1.3.



Figure 5.1: Simple sequential circuit consisting of three registers without clock gating.

5.1.1 Traditional Clock Skew Scheduling

In a sequential timing path P, assume R_i and R_j represent two registers, t_i and t_j are clock arrival times for registers R_i and R_j , respectively. For each data path P in the circuit, two types of timing constraints exist: setup time (max delay) and hold time (min delay) constraints, which are represented, respectively, by (5.1) and (5.2),

$$t_i - t_j \le T - DP_{max},\tag{5.1}$$

$$t_i - t_j \ge -DP_{min},\tag{5.2}$$

where *T* is the clock period, DP_{max} and DP_{min} are the maximum and minimum data path delays that include setup and hold time, respectively [62].

A simple sequential circuit with three registers R1, R2 and R3 and without clock gating is shown in Fig. 5.1. Two buffers B1 and B2 are inserted at the primary input and the output load, respectively. A pair of delay values (D_{min}, D_{max}) is denoted with each buffer, where $D_{min,buf}$ and $D_{max,buf}$ are the minimum and maximum propagation delay of the buffer, respectively. There are two data paths in this circuit, $R1 \rightarrow R2$ and $R2 \rightarrow R3$, which are also associated with a pair of delay values $(DP_{min,path}, DP_{max,path})$ representing minimum and maximum data path delays.

Conventional clock skew scheduling approaches find a set of clock arrival times

LP based formulation				
Oł	ojective: min T			
1	$-12 \le t_1 - t_2 \le T - 16$			
2	$-10 \le t_2 - t_3 \le T - 13$			
3	$-2 \le t_{host} - t_1 \le T - 4$			
4	$-5 \le t_3 - t_{host} \le T - 7$			
5	$0 \le t_1, t_2, t_3, t_{host} \le T$			

Table 5.1: LP based formulation of skew scheduling for the simple circuit shown in Fig. 5.1.

corresponding to each register, which should satisfy each data path's timing constraints represented by (5.1) and (5.2). In [76], the proposed clock skew scheduling methodology is formulated as a simple linear programming (LP) problem where the objective function is to minimize the clock period. The linear programming model of the motivational example shown in Fig. 5.1 is listed in Table 5.1. Lines 1 to 4 represent the timing constraints of the two data paths and the primary input and the primary output paths. Line 5 is included to limit the maximum global skew within one clock period. The linear programming determines the minimum clock period as 10 units with the following set of skew schedule: $t_1 = 0$, $t_2 = 6$, $t_3 = 9$ and $t_{host} = 6$.

In addition to utilizing linear programming to perform clock skew scheduling, a sequential circuit can also be modeled as a constraint graph G(V, E), in which each vertex represents a register and two edges (with opposite directions) connecting two vertices represent setup and hold time constraints, respectively. In [79], a constraint graph based approach is proposed to optimize clock skew. In this graph-based approach, each data path from R_i to R_j in a sequential path has two edges: 1) an edge (R_j, R_i) with weight $T - DP_{max}$ models the setup time constraint in (5.1) and



Figure 5.2: Constraint graph based formulation of skew scheduling for the circuit shown in Fig. 5.1: (a) constraint graph, (b) after applying a clock period of 10 units eliminating all of the negative weight cycles.

2) an edge (R_i, R_j) with weight DP_{min} models the hold time constraint in (5.2). In order to synchronize the primary input and the primary output, a special vertex *Host* is added. This constraint graph provides skew schedule only if no negative weight cycle exists in the constraint graph. The well-known Bellman-Ford algorithm [85] is utilized to detect a negative weight cycle and increase the clock period *T* until all of the negative weight cycles are eliminated.

Using the circuit of the motivational example in Fig. 5.1, the constructed constraint graph is shown in Fig. 5.2(a). The solid lines represent setup time constraints, and the dashed lines represent hold time constraints. After applying the graph-based method, a minimum clock period of 10 units (similar to LP result) is computed with the set of clock arrival times as: $t_1 = 1$, $t_2 = 7$, $t_3 = 10$ and $t_{host} = 7$. As depicted in Fig. 5.2(b), there is no negative weight cycle after substituting clock period with 10 units.



Figure 5.3: Integrated clock gating (ICG) cell.

5.1.2 Clock Skew Scheduling with Clock Gating

Clock gating is a popular technique to save dynamic power by deactivating the clock signal of the idle registers [15,16]. Typically, an integrated clock gating (ICG) cell, as shown in Fig. 5.3, is utilized to prevent the clock signal from switching. The enable pin within an ICG cell creates a clock enable (or control) path in addition to the data paths. Thus, a clock enable (or control) path refers to the combinational logic from the output pin of a register to the enable pin of an ICG cell.

In practice, one ICG cell gates multiple registers since an ICG cell placed at higher levels of a clock tree can save more dynamic power. Thus, in industrial designs, it is common to have *a local clock tree* between an ICG cell and the registers that are gated by this ICG cell. A *clock propagation path* on the local clock tree is therefore defined as the path from the output pin of an ICG cell to the clock pin of a register that is gated by this ICG cell. Since an ICG cell typically gates multiple registers, there are more than one clock propagation paths for an ICG cell. The delay of the clock propagation path (the delay between the clock arrival time to the ICG cell and the clock arrival time to the register gated by this ICG cell delay and is bounded by the longest path within the local tree. Thus,

each ICG cell is associated with a lower and upper bound of clock propagation path delay.



Figure 5.4: Simple sequential circuit consisting of an ICG cell, two registers gated by this ICG cell, a local clock sub-tree, and a timing loop formed by clock propagation path and clock enable path.

A simplified motivational example with clock gating is shown in Fig. 5.4 to better illustrate the aforementioned definitions. For simplicity, the circuit in this example has one ICG cell *ICG*1, gating two registers *R*1 and *R*2. A local sub-tree including two buffers *B*5 and *B*6 is synthesized to drive the two registers. Each buffer is denoted with a pair of delay values, which indicates the minimum and the maximum clock propagation path delays. The clock enable (or control) path is from *R*1 to *ICG*1 and consists of a single combinational gate, *C*1. Note that for simplicity, data paths are omitted in this example so that the issues related with clock gating can be emphasized.

Conventional clock skew scheduling methodologies cannot consider the unique challenges introduced by clock gating. In [86], the authors have recently proposed a linear programming approach to investigate the clock gated designs. In this work, useful skew is utilized in a gated design via considering both the data paths and clock enable paths with the objective function of minimum insertion delay [86]. However, it is assumed that the clock arrival time to an ICG cell is the same as the clock arrival time to the registers gated by this ICG. This assumption is impractical since in practice, the clock signal is distributed with a local clock tree that has larger and non-identical clock propagation delays (as depicted in Fig. 5.4). A method to perform clock skew scheduling in clock gated design with a local sub-tree is described in Section 5.2.

5.1.3 Low Swing Operation

In gated clock networks, each ICG cell creates a timing path for the *Enable* signals. Note that an ICG cell consists of a latch, as shown in Fig. 5.3. Unlike conventional data paths, the output of an *Enable* path is a clock signal. In practice, an ICG cell can drive a large number of flip-flops. Thus, it is common to have a local clock tree between the ICG and the sinks driven by this ICG. In Fig. 5.4, this local tree is simply represented by buffer B5 and B6.

When the clock voltage is reduced, the delay from ICG to the flip-flops (R2-R5) increases. Thus, clock signal arrives at ICG much earlier than the sinks R2-R5. Assuming negligible clock skew, clock signal arrives at R1 at approximately the same time as R2-R5. Thus, clock signal arrives at ICG (capturing latch of the *Enable* path) earlier than the R1 (launching flip-flop of the *Enable* path). Thus, the timing slack of the *Enable* path is *reduced* by this difference. This issue places a practical limitation on low voltage clocking if performance needs to be maintained.

To better illustrate this issue, signal waveforms at different clock nets and *Enable* signal are shown in Figure 5.5, assuming zero clock skew. During the second clock



Figure 5.5: Timing graph of the gated clock network shown in Fig. 2.13.

period, *Enable* signal changes. Referring to this figure, the *Enable* paths should satisfy the following max delay constraint,

$$t_{EN} + t_{ICG \ setup} + t_{clock \ propagation} < T_{clock}, \tag{5.3}$$

where t_{EN} , $t_{ICG \ setup}$ and $t_{clock \ propagation}$ are, respectively, *Enable* path delay, ICG cell setup time, and clock propagation delay within the local clock tree. The sum of these three variables should be less than one clock period. Since clock signal should always arrive at the ICG cell earlier than the flip-flops gated by this ICG cell (determined by $t_{clock \ propagation}$ that is always positive), the timing slack of the *Enable* path is reduced. In low swing operation, due to the increase in clock buffer delays, clock propagation delay $t_{clock \ propagation}$ increases. Thus, the reduction in the timing slack of the *Enable* path is more pronounced. The proposed linear programming based useful skew methodology makes low swing operation more practical by alleviating this timing degradation of the *Enable* paths.

5.2 Proposed Approach

Since ICG cell has a clock pin, in the proposed approach, each ICG cell is treated as a register with an associated clock arrival time. Since there is a local clock tree between an ICG cell and registers gated by this ICG, the associated clock propagation delays can be treated as clock skew. However, note that the clock signal should arrive to the ICG cell earlier than it arrives to the registers gated by this ICG cell due to positive clock propagation path delay. This constraint is different than conventional data paths where skew can be both positive and negative. Two different objectives are considered: (1) maximize circuit performance and (2) increase *Enable* path slack. These approaches are introduced in Section 5.2.1 and Section 5.2.2, respectively.

5.2.1 Maximizing Circuit Performance

The linear programming based solution to skew scheduling in gated clock trees is described in Section 5.2.1.1 whereas the constrained graph based approach is discussed in Section 5.2.1.2.

5.2.1.1 Linear Programming

The arrival time of a clock signal to a register gated by an ICG cell is larger than the arrival time of the clock signal to the ICG cell (see Fig. 5.4). The lower bound for each clock propagation path delay is determined by the AND gate delay and a local clock tree. This inequality is given by,

$$t_{icg,j} - t_i \le -CP_{min},\tag{5.4}$$

LP based approach for ICs with clock gating				
Objective: min T				
1 $t_i - t_j \ge -DP_{min}(data \ path)$				
2 $t_i - t_j \leq T - DP_{max}(data \ path)$				
3 $t_{icg,j} - t_i \ge -CP_{max}$ (propagation path)				
4 $t_{icg,j} - t_i \leq -CP_{min}$ (propagation path)				
5 $t_i - t_{icg,j} \ge -EP_{min}$ (enable path)				
6 $t_i - t_{icg,j} \leq T - EP_{max}$ (enable path)				
7 $0 \leq t_i, t_{icg, i} \leq T$				

Table 5.2: LP based approach to clock skew scheduling in a clock gated design.

where $t_{icg,j}$ and t_i are the clock arrival times to ICG cell ICG_j and register R_i , respectively. CP_{min} is the minimum clock propagation path delay.

An upper bound on clock propagation path delay is also required to represent the maximum delay of the local clock tree,

$$t_i - t_{icg,j} \le CP_{max},\tag{5.5}$$

where CP_{max} is the maximum delay of the corresponding clock propagation path. Combining the constraints in (5.4) and (5.5) with the traditional, data path related constraints, an improved linear programming solution for skew scheduling in ICs with gated clock trees is obtained, as listed in Table 5.2. The bold lines represent the *new* constraints required for gated clock networks.

The first two lines are the data path related constraints whereas lines 3 and 4 are the constraints related with clock propagation paths. Lines 5 and 6 represent the timing constraints of the enable (control) path. Line 7 is added to limit the global skew within one clock period. The linear programming based solution for

LP based approach for ICs with clock gating				
Objective: min T				
s.t. $-3 \leq t_{host} - t_1 \leq T - 5$				
$-2 \le t_{host} - t_2 \le T - 5$				
$-2 \le t_{host} - t_3 \le T - 5$				
$-5 \le t_2 - t_{host} \le T - 7$				
$-3 \le t_{icg,1} - t_2 \le -1$				
$-4 \le t_{icg,1} - t_3 \le -2$				
$-11 \le t_1 - t_{icg,1} \le T - 15$				
$-14 \le t_3 - t_{icg,1} \le T - 20$				
$0 \le t_1, t_2, t_3, t_{icg,1}, t_{host} \le T$				

Table 5.3: Application of the LP based approach to circuit shown in Fig. 5.4.

the motivational example in Fig. 5.4 is listed in Table 5.3. The program determines the minimum clock period as 22 units and a set of clock arrival times as $t_1 = 0$, $t_2 = 1$, $t_3 = 2$, $t_{icg,1} = 0$, and $t_{host} = 0$.

5.2.1.2 Constraint Graph

In addition to linear programming, constraint graph based solution is also proposed to compare the efficacy and confirm the accuracy of the proposed methods. Each ICG cell is treated as a register and added to the directed graph as a vertex. The maximum and minimum clock propagation path delays are treated, respectively, as setup and hold time constraints of a traditional data path. Specifically, (5.4) is treated as a setup time constraint and modeled by a directed edge (R_i , ICG_j) with weight $-CP_{min}$. Similarly, (5.5) is treated as a hold time constraint and modeled by a directed edge (ICG_j , R_i) with weight CP_{max} .

An important issue in graph based solution of skew scheduling in gated clock



Figure 5.6: Simple example to illustrate the timing loop formed by an ICG cell and a register gated by this ICG cell.



Figure 5.7: Constraint graph of the circuit shown in Fig. 5.6: (a) original graph, (b) after one iteration with clock period as 11 units, (c) after breaking the timing loop.

networks is a possible timing loop that can form between an ICG cell and one of the registers gated by this ICG cell. Assume that the enable signal of the ICG cell is provided from the output pin of one of the registers that is gated by the same ICG cell (such as *ICG*1 and *R*3 in Fig. 5.4), then the ICG cell and the register form a loop. Unlike conventional data paths, the clock signal should arrive to the register *later* than it arrives to the ICG. Thus, this timing loop should be broken from the directed graph while still maintaining accurate results. As observed from experimental results on ISCAS'89 benchmark circuits, breaking the loop is necessary to obtain a feasible skew schedule.

To better describe this issue, consider the example shown in Fig. 5.6 where the enable signal of *ICG*1 is generated by the output signal of *R*1, forming a timing loop. The constraint graph of this circuit is depicted in Fig. 5.7. Due to the loop, there are two sets of max and min delay constraints: 1) $t_{icg,1} - t_1 \le -2$, $t_{icg,1} - t_1 \ge -5$ and 2) $t_1 - t_{icg,1} \le T - 9$, $t_1 - t_{icg,1} \ge -6$, as shown in Fig. 5.7(a). To break the loop, only the tighter constraints of the same directed edge (*i.e.* smaller weight) should be preserved. For example, assume that in one of the iterations, clock period *T* is determined as 9 units, producing the following inequalities: $-5 \le t_{icg,1} - t_1 \le -2$ and $0 \le t_{icg,1} - t_1 \le 6$, as shown in Fig. 5.7(b). Since only the tighter constraint of the same edge should be preserved, the edges with weights 5 and 6 are dropped, breaking the loop, as shown in Fig. 5.7(c). According to Fig. 5.7(c), a negative weight cycle exists, indicating that the chosen clock period should be increased. If the process is repeated with a clock period of 11 units, the cycle weight becomes zero, indicating that the minimum clock period has been determined while satisfying the timing constraints.

The pseudo-code of the proposed constraint graph based solution is provided in Table 5.4. The algorithm takes the timing data as the input and generates a constraint graph in lines 2 to 12. In lines 3 to 5, the timing loops formed by ICG cells and registers gated by the same ICG cells are detected and broken by the proposed method (*i.e.*, preserving only the smaller weight of the same directed edges). In line 13, Bellman-Ford algorithm [85] is utilized to detect negative weight cycles. If found, clock period is increased until all of the negative weight cycles are removed. In line 18, the algorithm returns the minimum clock period and the skew schedule, *i.e.*, clock arrival time to each register and ICG cell.

As an example, the proposed algorithm is applied to the circuit shown in Fig. 5.4.

	Graph based approach (timing data)
1:	start with a clock period T
2:	for each edge(u,v) with weight w
3:	if $(u,v) \exists$ in G(V,E)
4:	if weight(u,v)>w
5:	weight(u,v)=w
6:	else
7:	add edge(u,v)
8:	end for
9:	add a source node
10:	for each $V \in G(V,E)$ except source node
11:	add edge(source,V) with weight T
12:	end for
13:	apply Bellman-Ford algorithm on G(V,E)
14:	if \exists negative weight cycle
15:	increase clock period
16:	repeat Line 1-13
17:	else
18:	return clock period T and skew schedule

Table 5.4: Graph based solution for ICs with clock gating, including the proposed mechanism to break the timing loop.



Figure 5.8: Constraint graph of the circuit shown in Fig. 5.4: (a) original graph, (b) after one iteration with clock period as 22 units, (c) after breaking the timing loop.

The original constraint graph that corresponds to this circuit is depicted in Fig. 5.8(a). *T* is replaced with the minimum clock period 22 units, producing the graph shown in Fig. 5.8(b). The timing loop formed by *ICG*1 and *D*3 are broken using the proposed method, producing the final graph shown in Fig. 5.8(c). The algorithm returns the clock arrival times as $t_1 = 22$, $t_2 = 22$, $t_3 = 22$, $t_{icg} = 20$, and $t_{host} = 22$.

5.2.2 Increasing Timing Slack of *Enable* Paths

LP based approach for ICs with clock gating				
Inputs: path delays and clock period				
Outputs: skew schedule				
Objective: max $\Sigma(t_{reg,i} - t_{icg,j})$ for each j				
1 $t_i - t_j \ge -DP_{min}(data \ path)$				
2 $t_i - t_j \leq T - DP_{max}(data \ path)$				
3 $t_{icg,j} - t_i \ge -CP_{max}(propagation path)$				
4 $\mathbf{t_{icg,j}} - \mathbf{t_i} \le -\mathbf{CP_{min}}(\mathbf{propagation path})$				
5 $\mathbf{t_i} - \mathbf{t_{icg,j}} \ge -\mathbf{EP_{min}}(\mathbf{Enable \ path})$				
6 $\mathbf{t_i} - \mathbf{t_{icg,j}} \le \mathbf{T} - \mathbf{EP_{max}}(\mathbf{Enable \ path})$				
7 $0 \leq t_i, t_{icg,j} \leq T$				

Table 5.5: Proposed LP based approach to exploit useful skew in low swing operation.

The previous section provided a framework to achieve skew scheduling in gated clock trees. In this section, this framework is utilized to exploit useful skew in increasing the timing slack of the *Enable* paths. As described earlier, in gated low voltage clock trees, the *Enable* paths suffer from reduced timing slack. In this section, the objective function of the LP is to maximize the ICG-to-DFF delay, thereby increasing the timing slack of the *Enable* paths, as shown in Table 5.5. In

other words, more delay can be tolerated between ICG and flip-flops.

The linear programming based solution for the motivational example in Fig. 5.4 is listed in Table 5.6 after substituting clock period with 22 time units. The program determines a set of clock arrival times as $t_1 = 8$, $t_2 = 22$, $t_3 = 21$, $t_{icg,1} = 19$, and $t_{host} = 20$, where *ICG*1 to *R*2 delay increases from 1 to 3 time units, whereas *ICG*1 to *R*3 delay remains the same as 2 time units.

LP based approach for ICs with clock gating			
Objective: max $(t_2 - t_{icg,1} + t_3 - t_{icg,1})$			
s.t. $-3 \le t_{host} - t_1 \le 17$			
$-2 \le t_{host} - t_2 \le 17$			
$-2 \le t_{host} - t_3 \le 17$			
$-5 \le t_2 - t_{host} \le 15$			
$-3 \le t_{icg,1} - t_2 \le -1$			
$-4 \le t_{icg,1} - t_3 \le -2$			
$-11 \le t_1 - t_{icg,1} \le 7$			
$-14 \le t_3 - t_{icg,1} \le 2$			
$0 \le t_1, t_2, t_3, t_{icg,1}, t_{host} \le 22$			

Table 5.6: Application of the LP based approach to circuit shown in Fig. 5.4 to increase the timing slack of the Enable paths.

5.3 Experimental Results

5.3.1 Circuit Performance

The proposed LP based and constraint graph based approaches for skew scheduling in gated clock networks are evaluated using the largest ISCAS'89 benchmark circuits consisting of up to approximately 2000 registers. Each benchmark is synthesized with Synopsys Design Compiler [87] using the 45 nm NanGate open cell library [88]. ICG cells are inserted by the tool during the synthesis stage. An open source GLPK (GNU Linear Programming Kit) [89] is used as the linear programming solver, running on a Linux system with Intel Xeon processor.

The experimental results are listed in Table 5.7 for both linear programming and graph based solutions. It is important to note that both solutions provide the same minimum clock period in each circuit, verifying the accuracy of the algorithms. The maximum reduction in clock period after skew scheduling is approximately 21%, which highly depends upon the timing data. In some benchmarks, higher gating percentage corresponds to less reduction in clock period, such as S1423 and S38417. However, this behavior does not hold in other benchmarks such as S38584 where 16% reduction in clock period is achieved with approximately 72% gating. It is also shown in Table 5.7 that the graph based solution produces smaller global skew than LP based solution.

The run time of both solutions is compared in Fig. 5.9 for some of the benchmark circuits. LP based solution runs faster than or equal to graph based solution. Note that the graph based approach utilizes Bellman-Ford algorithm with a computational complexity of $O(V \cdot E)$ [85], where V is the overall number of registers and ICG cells in the circuit, and E is the overall number of data paths, *Enable* paths and clock propagation paths. Lines 2 to 8 in Table 5.4 have a complexity of O(E) and lines 9 to 11 have a complexity of O(V). Therefore, the computational complexity of the graph based method is maintained at $O(V \cdot E)$. The LP based solution utilizes the simplex algorithm and in practice, runs faster. However, note that with certain inputs, simplex algorithm may require exponential time to reach a solution [85].

Table 5.7: Experimental results demonstrating the reduction i clock skew scheduling (CCS).	in clock period of gated ISC	AS'89 benchmark circuits afte

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Circuit	No of DEE	No. of ICG.	Gatinado	Ū	ock Period (n	(S)	Max Glc	bal Skew (ns)
CIICUII	STIT IN ONI			Zero Skew	After CSS	Reduction	LP	Graph
S1423	74	30	90.54%	4.9212	4.6618	5.27%	0.2594	0.2374
S9234	125	15	51.20%	2.9278	2.7369	6.52%	0.7171	0.1909
S13207	240	37	44.17%	2.4436	2.0678	15.38%	0.3897	0.3896
S15850	434	57	66.36%	4.9466	4.1436	16.23%	0.8030	0.1342
S35932	1728	4	0.23%	3.8314	3.0419	20.61%	0.7895	0.0773
S38417	1459	236	49.62%	4.8895	4.6490	4.92%	0.2926	0.2487
S38584	1240	251	71.61%	4.5806	3.8425	16.11%	0.7381	0.0570



Figure 5.9: The runtime comparison of linear programming and graph based approaches.

5.3.2 Timing Slack of *Enable* Paths

The proposed useful skew approach to facilitate low swing clocking without degrading the timing slack of the *Enable* paths is evaluated with the same software setup as in maximizing circuit performance. The longest runtime is 120 seconds for s38417.

The experimental results comparing the zero skew and useful skew are listed in Table 5.8. Both zero skew and useful skew cases operate at the same clock period which is the minimum clock period in zero skew. Depending upon the mismatch in the data paths, up to 86% improvement in *Enable* slack can be achieved. On average, the slack of the *Enable* path is increased by 47% after applying the proposed useful skew approach.

The maximum ICG-to-DFF delays are listed in Table 5.9 when the clock period is the minimum theoretical clock period *after useful skew*. If the proposed useful

Circuit	Clock Period	Max ICG-to-DFF Delay (ns)		Increase in
Circuit	(ns)	Zero Skew Useful Skew		Enable Slack
s13207	2.71	2.13	2.36	10.8%
s15850	4.93	2.78	3.72	33.8%
s35932	3.83	1.20	2.24	86.7%
s38417	4.85	3.47	4.85	39.8%
s38584	4.61	2.12	3.48	64.2%

Table 5.8: Experimental results demonstrating the increase in the slack of the *Enable* paths after exploiting useful skew.

Circuit	Min Clock Period	Max ICG-to-DFF Delay	Run Time
	(ns)	(ns)	(s)
s13207	2.26	1.91	0
s15850	4.13	2.91	5
s35932	3.04	1.45	7
s38417	4.66	4.56	120
s38584	4.04	2.92	25

Table 5.9: Experimental results demonstrating the increase in the slack of the *Enable* paths after exploiting useful skew at the minimum clock period.

skew approach is adopted in this case, the maximum ICG-to-DFF delays are degraded on average, by 20% as compared to the useful skew case in Table 5.8 (with a larger clock period). This result is expected since in Table 5.9, there is a tighter constraint for clock period.

5.4 Summary

A useful skew approach in clock-gated network is proposed in this chapter to maximize the circuit performance and increase the timing slack of *Enable* path, which facilitates low swing clocking. It is evaluated on ISCAS'89 benchmark cir-

cuits with clock gating cell inserted automatically by Synopsys Design Compiler. Experimental results demonstrate up to approximately 21% reduction in clock period and 47% increase in the timing slack of the *Enable* path.

Chapter 6

Slew-Driven Clock Tree Synthesis Methodology

The design process for clock distribution networks is directly affected by technology (*i.e.* interconnect and transistor) scaling [5, 11, 90]. The impact of technology scaling on clock skew is well-understood and the skew constraint is satisfied with various existing clock tree synthesis (CTS) algorithms [28, 91–97]. Alternatively, the methodical investigation of clock slew is primarily unaddressed. In particular, the increase in the interconnect resistance makes it more challenging to satisfy slew constraints on long wires. Furthermore, voltage scaling is a popular method for power management, which also exacerbates clock slew.

Despite the well-understood detrimental effects of interconnect resistance and low voltage operation on clock slew, using clock slew as a driving factor for clock tree synthesis has not been investigated. In [95], an obstacle-avoiding and slewconstrained clock tree synthesis methodology with efficient buffer insertion is proposed, where clock skew and latency are enhanced. In [96], a fast power- and slewaware gated clock tree synthesis methodology is proposed with zero skew. In [29], a variation-aware clock network design methodology is proposed for ultra-low voltage circuits, where both clock skew and slew are controlled to maximize the circuit performance. In [27], a systematic approach is proposed to design the clock tree for subthreshold circuits to reduce the clock slew variations while minimizing the energy dissipation in the tree. Exploiting slew-awareness as part of the clock tree synthesis (*i.e.* slew-driven) has not been previously addressed.

A slew-driven CTS methodology called SLECTS is proposed in this chapter. SLECTS can satisfy aggressive slew constraints that are significantly more challenging for traditional delay/skew-driven CTS methodologies.

Instead of targeting skew minimization as the primary objective and resolving slew violations with buffer insertion with a capacitance or slew bound, as in traditional skew-driven CTS, SLECTS targets slew optimization at each stage of the synthesis, such as clustering (*i.e.* merging) clock tree nodes, defining routing points and handling long interconnects. A typical approach in existing CTS techniques is to perform skew minimization in the first stage and resolve slew violations during post-CTS optimization [98]. Skew-driven CTS uses buffering and sizing to constrain only skew during the CTS process, and uses additional buffering and sizing post-CTS to remove slew violations. Alternatively, SLECTS uses buffering and clustering more efficiently to simultaneously constrain skew and slew. Due to this efficient slew handling and efficient use of buffering, SLECTS leads to reduced power dissipation while satisfying the slew and skew constraints. The proposed slew-driven CTS methodology exhibits the following innovations: 1) a new merg-ing point computation method, 2) a new method to simultaneously check and satisfy skew and slew, 3) a new cost metric for the merging process, 4) a new net splitting method, which is essential for clock trees with long interconnects.

Merging point computation and cost metric novelties help reducing the power consumption compared to existing methods. In addition, SLECTS is significantly more successful in satisfying tighter slew constraints at lower operating voltages. Thus, SLECTS not only enables clock signals with higher frequencies (where slew constraints are tighter) to be reliably distributed, but also accomplishes this distribution with reduced power consumption.

Experimental results on an industrial circuit with more than 1 million gates in 28 nm FDSOI technology demonstrate that, at the slow process, voltage, temperature corner, SLECTS satisfies tight slew constraint of 60 ps whereas a commercial CTS tool not only violates the slew constraint, but also consume 8% more clock power. At the scaled 0.8 V operation, SLECTS satisfies the slew constraint with approximately 15% less clock power while achieving a similar skew constraint. The experimental results demonstrate that SLECTS methodology can be combined with the proposed low swing flip-flop topology (see Chapter 3) to produce a low swing/voltage clock tree with up to 48% reduction in clock power.

The rest of this chapter is organized as follows. Five proposed techniques for the slew-driven clock tree synthesis methodology are introduced in Section 6.1. Experimental results of the proposed methodology are presented in Section 6.2. The power analysis of combining SLECTS and low swing flip-flop is provided in Section 6.3. Finally, the chapter is concluded in Section 6.4.

6.1 Slew-Driven Clock Tree Synthesis Algorithm

Deferred merge embedding (DME) method is a popular framework used for clock tree synthesis in the literature [43, 44, 93]. The proposed methodology, developed within the DME framework, is illustrated in Fig. 6.1 with a flowchart. The slew driven novelties in SLECTS are highlighted with labels Step 1, Step 2, Step 3, Step 4 and Step 5. In particular, SLECTS consists of 5 novel contributions:

- 1. A slew- and skew-aware merging point computation method (Step 1),
- 2. Checking and satisfying skew using a single or multiple buffers (Step 2),
- 3. Checking and satisfying slew using buffer sizing (Step 3),
- 4. A pair selection and cost metric definition considering physical distance for efficient sink clustering (Step 4),
- 5. A slew- and insertion delay-aware net splitting (Step 5).

These five steps are described in Sections 6.1.1 to 6.1.5. Time complexity and runtime of the proposed method are discussed and compared with a commercial tool in Section 6.1.6.

6.1.1 Step 1: Merging Point Computation

In traditional DME method, the algorithm searches every pair i - j from the unmerged nodes to find feasible pairs to merge. A merging point is calculated for each such pair i - j as a virtual routing point. A common practice [94] is to select a specific point for merging considering skew, using the zero-skew-tree DME (ZST-DME) algorithm [43,44]. Another approach proposed in [47] develops a bounded-skew-tree DME (BST-DME) to define merging regions considering the



Figure 6.1: The flowchart of SLECTS. The blue boxes are executed in every *foreach* loop, and the red boxes are executed after an iteration of *foreach* loop is finished.

skew constraint during the bottom-up phase, and chooses the minimum wirelength point at each region during the top-down phase. This early approach is applicable only in "unbuffered" clock routing. In practice (and literature), buffered clock tree routing has long been the norm [94, 99, 100], particularly when satisfying the slew constraint is critical. Another practice is to use ZST-DME or BST-DME approaches as a first step, while allowing slew violations, and consider buffering as an added optimization step to remove violations. In slew-driven buffering, computing merging regions at each iteration of the bottom-up phase is computationally expensive due to the highly complex slew estimation equation (introduced in Section 6.1.1). Furthermore, permitting slew violations results in decisions based on inaccurate(ly high) slew on the nodes with violations.

In this thesis, the skew constraint-based merging regions are constructed during the bottom-up phase, similar to the BST-DME methodology [47]. Unlike BST-DME methodology where merging regions are propagated during the bottom-up phase and the merging points are determined during the top-down phase, the merging point is determined within this merging region considering the slew constraint *during the same phase*. This is an algorithmic change from traditional approaches in order to simultaneously satisfy skew and slew constraints. This process requires a novel definition for permissible merging window to satisfy the skew constraints, and cross-referencing this window with a minimum slew point to satisfy the slew constraint.



i-----j EP1 EP2

(a) EP1 and EP2 intersect with pair i - j.



(b) EP1 and EP2 do not intersect with pair i - j.



(c) Minimum slew point is within the permissible merging window, it is set as the merging point.

(d) Minimum slew point is outside the permissible merging window, the closest end point is set as the merging point.

Figure 6.2: Permissible merging window and minimum slew point definitions to identify the merging point.

The zero skew merging point is computed as follows [94]:

$$L_{i} = \frac{0.5C_{unit}L(i,j)^{2} + L(i,j)C_{j}}{C_{i} + C_{j} + L(i,j)C_{unit}} + \frac{t_{j} - t_{i}}{R_{unit}(C_{i} + C_{j} + L(i,j)C_{unit})},$$
(6.1)

where L(i, j) is the distance between two nodes (μ m), R_{unit} and C_{unit} are the per unit resistance (Ω/μ m) and capacitance (fF/μ m) of the interconnect, respectively, t_i and t_j are the insertion delay from i and j to their sinks, respectively, C_i and C_j are the capacitance at nodes i and j, respectively. Note that to improve insertion delay accuracy, SLECTS computes the effective capacitance and considers resis-

Algorithm 1 Merging Point Computation

1: $Max_i = max[D_{ins}(i)]$ 2: $Max_j = max[D_{ins}(j)]$ 3: $Min_i = min[D_{ins}(i)] + skew_{const}$ 4: $Min_i = min[D_{ins}(i)] + skew_{const}$ 5: Compute EP₁ by computing L_{EP1} with (6.1) for $t_i = Max_i$, $t_j = Min_j$ 6: Compute EP₂ by computing L_{EP2} with (6.1) for $t_i = Min_i$, $t_i = Max_i$ 7: Compute EP1 and EP2 intersection with pair i - j as permissible merging window 8: *Compute min slew point m by solving (6.4)* 9: if $m \in permissible$ merging window then *Merging point* k = m10: 11: else if m < EP1 then 12: Merging point k = EP113: else *Merging point* k = EP214: 15: end if

tive shielding (based on [101]) to bi-linearly interpolate the look-up tables for each clock buffer. As such, node capacitances C_i and C_j in (6.1) represent the effective capacitance.

The proposed merging point computation algorithm is presented in Algorithm 1. For each pair *i*-*j*, the *permissible merging window* is defined based on the skew constraint. As mathematically described in Algorithm 1, each end point (*EP*₁ and *EP*₂) represents a corner case where the skew between *i*-*j* pair is equal to skew constraint *skew_{const}*, and any point within the permissible merging window satisfies this constraint (i.e. \leq *skew_{const}*). In literature, there are studies that aim to choose the middle of the permissible merging window as the merging point so as to increase the robustness of delivered skew to variations [102]. In this work, the objective is to simultaneously constraint skew and slew. As such, a slew-driven metric for merging point computation is defined, as described below. According to Algorithm 1, two skew corners and a permissible merging window is generated along the axis of the *i*-*j* pair using (6.1) (Lines 5-7). The permissible merging window is a line of potential merging points along which the skew constraint is satisfied. If the two skew corners *EP*1 and *EP*2 intersect with pair i - j, the permissible merging window is set as the intersection, as shown in Fig. 6.2(a). Alternatively, if the two skew corners are outside the pair i - j, as shown in Fig. 6.2(b), the permissible merging window is set based on the two corners. In this case, buffer insertion (when the delay mismatch is larger than one clock buffer delay) or wire snaking (when the delay mismatch is smaller than one clock buffer delay) is applied to fix skew. Fixing skew with single/multiple buffer insertion is described in Section 6.1.2. After the permissible merging window is generated, the *minimum slew point* is computed (Line 8). The minimum slew point is defined as the point that makes the slew at node *i* and *j* equal and minimum. In order to determine this point, the PERI model [103] is used for slew propagation, which estimates the slew degradation *S*(*W*) on a wire segment *W* as:

$$S(W) = ln(9) \times ED(W), \tag{6.2}$$

where ED(W) is the Elmore delay [104] of the wire segment *W*. The output slew $S_{out}(W)$ of a wire segment *W* is estimated as:

$$S_{out}(W) = \sqrt{S_{in}(W)^2 + S(W)^2},$$
 (6.3)

where $S_{in}(W)$ is the input slew of the wire segment. Using (6.2) and (6.3), the

minimum slew point *m* should satisfy the following equation:

$$S_i^2 - (ln(9) \times ED(m,i))^2 = S_j^2 - (ln(9) \times ED(m,j))^2,$$
(6.4)

where S_i and S_j are the target slew values at nodes *i* and *j*, respectively. The target slew values are set to slew constraint *slew_{const}* at the sink level, and they are propagated bottom-up to the internal nodes after each merging. After (6.4) is reorganized in a closed-form, it becomes a third-order equation (as Elmore delay scales quadratically with wirelength). By using first-order derivative and analyzing the monotonicity, one or multiple real roots can be found. If multiple real roots exist, the root that generates the minimum skew between pair i - j is selected as the minimum slew point *m*. If *m* is within the permissible merge window, it is set as the merging point *k*, as shown in Fig. 6.2(c). Alternatively, if *m* is outside the permissible window, *the closest end point of the permissible window* is set as the merging point *k* (Line 11-14), as shown in Fig. 6.2(d).

6.1.2 Step 2: Fixing Skew Using Buffer Insertion

After computing the merging point for each pair i - j, as described in Section 6.1.1, skew and slew constraints should be checked before determining the feasible pairs to merge. Skew-driven CTS uses buffering and sizing during the synthesis process to constrain clock skew. Since traditional DME-based CTS algorithms consider buffer insertion at the merging point only, slew violation can happen when the inserted buffer drives a long interconnect. These slew violations are typically fixed with a post-CTS optimization in traditional methods.

SLECTS considers both slew and skew constraints while constructing the clock



Figure 6.3: Illustration of fixing skew using single or multiple buffers and determining the new merging point after fixing skew.

tree in a bottom-up manner. In cases where the permissible merge window does not intersect with the i - j pair [see Fig. 6.2(b)], single or multiple buffers are inserted and evenly distributed to fix skew (move the merge point between nodes *i* and *j*), as depicted in Fig. 6.3.

If insertion delay mismatch between i - j is large or interconnect length between i - j is short, multiple buffers can be inserted. In this case, SLECTS distributes these buffers evenly while considering the capacitive load and maximum drive ability of each buffer. In Fig. 6.3, the capacitive load of *buffer 1* is the sum of load at node *i* and the interconnect capacitance of wire length *L*1. For the remaining buffers, the capacitive load is the sum of buffer gate capacitance and the interconnect capacitance of wire length *L*2. If node *i* exhibits a large capacitive load, then the first buffer will be inserted sufficiently close to node *i*. This skew fixing algorithm is shown in Algorithm 2. The proposed approach computes the maximum interconnect length that each clock buffer in the library can drive, given the buffer gate capacitance (Line 4). Then, the overall buffer and interconnect delay is computed from node *i* with slew propagation from the input pin of last inserted

Algorithm 2 Fix Skew

1: $load_{first} = C_i + C_{L1}$ 2: $load_{other} = C_{gate} + C_{L2}$ 3: Find each type of buffer look-up tables 4: Compute L1 and L2 5: Propagate slew from the input pin of last inserted buffer 6: $D_{total} = \sum_{each \ buffer} (D_{buffer} + D_{wire})$ 7: if single buffer can fix the skew then return with buffer location and type 8: 9: else if multiple buffers can fix skew then return with buffer locations and types 10: 11: else Find minimum skew with single/multiple buffers 12: 13: end if

buffer (Line 5-6). After the overall delay is calculated, a new merging point between last inserted buffer and node j is computed with the proposed merging point computation algorithm described in Section 6.1.1. If single or multiple buffers can fix the skew violation, then buffer locations and types are stored (Line 7-10). Alternatively, if skew cannot be fixed by only inserting buffers, the minimum possible skew is determined (Line 12).

6.1.3 Step 3: Fixing Slew Using Buffer Sizing

In traditional skew-driven CTS, slew violations are typically fixed during post-CTS optimization. Since SLECTS targets slew optimization at every stage of the clock tree synthesis, it checks slew constraint with buffer sizing after checking/fixing skew violations with buffer insertion.

To satisfy the slew constraint for a specific pair i - j, a clock buffer is inserted at the merging point to drive the capacitive load. The buffer sizing algorithm to satisfy
Algorithm 3 Fix Slew

1: $load = C_i + C_j + C_{wire}$ 2: for each usable buffer size k do 3: Compute buffer output slew Slew_{out}(buf_k) 4: Propagate slew to i and j with (6.3) 5: if Slew_i \leq Slew_{iReq}&&Slew_j \leq Slew_{jReq} then 6: return buffer type k 7: end if 8: end for 9: slew cannot be fixed

slew constraint is described in Algorithm 3. In Lines 1-3, overall capacitive load at the buffer output pin is computed and the buffer output pin slew is determined using look-up table of the specific buffer size k and bi-linear interpolation. Then, buffer output pin slew is propagated to nodes i and j, using (6.3) (Line 4). Since slew is propagated bottom-up, the slew requirement of node i and j is checked. If the propagated slew from buffer output pin satisfies both node i and j slew requirement, then the specific buffer size k can drive the load at the merging point. Otherwise, a buffer with stronger drive capability is chosen (Line 5).

6.1.4 Step 4: Finding Feasible Pairs to Merge

According to Fig. 6.1, in SLECTS, no pairs are actually merged until after all of the i - j pairs are visited and a related cost is determined for each pair. The selection of pairs to merge and the cost definition significantly affect the quality of results. Thus, several pair selection techniques and cost definitions were introduced in the literature, which are classified into 2 groups: 1) distance-based [93], and 2) delay-based [94]. Distance-based approach considers the physical distance between two nodes as a cost metric, and merges minimum distance pairs. In terms of

accuracy, distance-based merging pair selection suffers from the deficiencies of using length as a delay metric. The time complexity of distance-based approach [93] is O(nlogn), as merging is performed by selecting all minimum distance pairs in one iteration. However, as the pairs are not selected one at a time, the merging of a new node (created by a previous merging) with an existing node is not considered. Thus, this selection results in a sub-optimal clustering.

The more contemporary and common cost definition is the delay-based approach, which achieves higher accuracy in terms of satisfying skew, the primary objective of traditional skew-driven CTS algorithms. Delay is typically estimated with Elmore delay, and common merging pair cost computations consider potential wire-snaking between candidate nodes, as well. The delay-based approach in [94], for instance, first identifies the candidate merging node with the maximum delay target (i.e. candidate node with the minimum insertion delay from the node to the clock sinks in its downstream). The approach then finds a minimum cost pair for this node where cost is defined as the Elmore delay to a candidate pair node, including the distance added to perform potential wire snaking. This approach provides better skew results (compared to [93]), however, restricting the selection of the minimum insertion delay node does not guarantee the minimum distance selection, thereby degrading clock slew. In terms of algorithmic complexity, the maximum delay target node and its minimum pair are identified with a linear search [both O(n) complexity], resulting in a complexity of $O(n^2)$.

The contemporary and common delay-based cost definitions in the merging pair selection has two drawbacks making them formidable for SLECTS: 1) Delay-based cost results in pairing nodes that are physically farther to minimize skew, which is detrimental to slew, 2) Considering wire snaking as part of cost metric is inaccurate.

Wire snaking is detrimental to slew, therefore, buffer insertion is a more viable option for merging pairs that require significantly high wire snaking.

Consequently, in this thesis, a distance-based approach (similar to [93]) is selected as the cost metric favoring reduced slew degradation along the path. It is important to note here that using a distance-based cost results in several subtree clusters that have different capacitance and delay values. This would make merging more difficult at the top-level of a clock tree due to the insertion delay mismatches. However, the potential effects of these mismatches are fixed by buffer insertion and/or wire snaking, and the power overhead of these processes are shown, experimentally, to be less than those necessary to fix slew following a traditional skewdriven CTS application through DME.

In SLECTS, the distance-based cost metric for clustering (merging) nodes is defined as *the sum of distance (i.e. wire length) from calculated merging point (see Section 6.1.1, Step 1) to node i and j (see Fig. 6.2).* This change from traditional DME-based CTS routines ensures satisfying both slew and skew constraints.

Algorithmically, the merging pair selection in SLECTS is performed by considering all of the possible pairs (up to n^2 possibilities) at each iteration (see the flowchart in Fig. 6.1). This theoretical $O(n^3)$ complexity of this selection scheme is avoided with data re-use. In the first iteration, the costs of all n^2 pairs of initial nnodes are computed [complexity of $O(n^2)$]. Starting from the second iteration, only the costs of merging the recently added node against the other (n-1) nodes [O(n)]are computed [complexity of $O(n^2)$] as the other pairing combinations are already computed in the first iteration. Thus, although the asymptotic complexity is still $O(n^3)$, the algorithm performs $O(n^2)$ computations and $O(n^3)$ look-ups. It is shown in Section 6.2 that the run time of the proposed methodology is significantly less



Figure 6.4: Demonstration of slew-aware net splitting.

than commercial CTS tools.

After finding the feasible pair, if merging this specific pair requires buffer insertion to fix slew or skew (as determined in Steps 2 and 3), it affects the slew of the downstream nodes. Therefore, a top-down slew propagation process is executed and slew values are updated to improve slew estimation and insertion delay accuracy.

6.1.5 Step 5: Slew-Aware Net Splitting

Traditional DME-based CTS algorithms consider buffer insertion only at the merging points, and do not consider splitting the net (i.e. with buffering) after selecting merging pairs. This approach produces slew violations on long interconnects and do not permit the desired voltage and frequency scaling. Thus, existing contemporary approach is to synthesize clock tree with slew violations and fix these violations as a post-CTS optimization.

SLECTS satisfies slew constraints while considering the insertion delays of the

Algorithm 4 Net splitting

1: $Cost_{curr} = \infty$ 2: **for** (*i*, *j*) in Unmerged nodes **do** if $Cost(i, j) < Cost_{curr}$ then 3: $Cost_{curr} = Cost(i, j), s_i = i, s_j = j$ 4: end if 5: 6: end for 7: **if** $D_{ins}(s_i) < D_{ins}(s_j)$ **then** Compute maximum interconnect length L with s_i 8: 9: **else** Compute maximum interconnect length L with s_i 10: 11: end if 12: Generate new node m at the computed location

nodes to be merged. The purpose of considering insertion delays is to avoid a high buffering and wire snaking cost that is induced due to large insertion delay mismatch, and keep number of buffer levels balanced for process-voltage-temperature (PVT) variations. In order to highlight this phenomenon, a motivational example is illustrated in Fig. 6.4. It is assumed that three nodes i, j and k are to be merged and a single buffer insertion cannot satisfy the slew constraint at neither of the nodes. Thus, the net of the selected pair of nodes needs to be split with buffer insertion to satisfy slew constraint. Assume that i-j pair has the lowest cost (i.e. minimum distance as defined in Section 6.1.4), and therefore is selected to be merged. A naive approach, depicted in Fig. 6.4(a), could start splitting from node i in order to bring the merging point closer to j and k for a lower merging cost in the next iteration. However, this would significantly increase the insertion delay at node i, resulting in excessive buffering and/or wire snaking when merging i with other nodes. The insertion delay-aware net splitting technique, presented in Algorithm 4, is proposed to address this issue. The proposed approach first finds the minimum cost pair (s_i and s_j in Line 4) and determines which node of the selected (i.e. minimum cost) pair has a smaller insertion delay. Then, the distance is computed from this lower insertion delay node (either s_i in Line 8 or s_j in Line 10) to generate a new node *m* (Line 12). Starting net splitting from the node that has a smaller insertion delay provides a more balanced buffering, such as the one depicted in Fig. 6.4(b).

In the proposed approach, the splitting point is determined as the longest feasible distance from the selected (smaller insertion delay) node. The longest feasible distance is computed using the slew constraint, the look-up tables of the buffer and the interconnect metrics (per-unit resistance and capacitance). Given a proper set of initial interconnect lengths, the algorithm can compute the longest feasible distance with a complexity of O(logn).

6.1.6 **Runtime and Computational Complexity**

Since the runtime of the algorithm has quadratic dependence $[O(n^2)]$ on circuit size, SLECTS should be optimized for large designs with tens of thousands of sinks and clock gating cells. Furthermore, note that if a buffer is inserted during skew or slew fixing (in Steps 2 and 3) while constructing the clock tree bottom-up, the insertion delay of the downstream nodes is affected since slew propagates top-down. Thus, after each buffer insertion, the slew is propagated starting from the inserted buffer input pin to enhance delay and skew accuracy. This process also increases the overall runtime.

To reduce the runtime, the traditional K – mean clustering [105] is applied to cluster a clock pin with large fanout. If a subtree fanout is over the average cluster size, K – mean clustering is applied, generating multiple clusters. The complexity is reduced from $O(n^2)$ to $O(n^2/K^2)$, where K is the number of clusters.



Figure 6.5: Runtime comparison of SLECTS and a vendor tool for three circuits described in Section 6.2.

The runtime comparison between a vendor CTS tool and SLECTS is illustrated in Fig. 6.5 for three designs of various sizes (see the following section). Both vendor tool and SLECTS run on a Linux platform with an Intel Xeon processor. According to Fig. 6.5, SLECTS runs more than 2X faster than the vendor tool, making it highly applicable to very large designs.

6.2 Experimental Results on an Industrial Processor

The proposed slew-driven clock tree synthesis methodology is implemented with C++. The sink, integrated clock gating cell, and clock logic cell locations are extracted from placed design database. SLECTS also requires clock constraints such as slew and skew, technology related parameters such as per unit interconnect resistance and capacitance, and characterization file (look-up tables) for clock buffers within the library.

After clock tree synthesis, SLECTS generates two files: 1) a *tcl* script with the type and location of clock buffers that are inserted throughout the clock tree, 2) a SPICE netlist of the clock tree for timing and power analysis based on the provided timing library and technology related parameters.

SLECTS is evaluated with three circuits of varying sizes ranging from 5K to over 1M gates (including an industrial processor), as listed in Table 6.1. The s38584 ISCAS'89 benchmark and 64-point FFT core [106] are implemented in a 45 nm CMOS technology [107] and operate at 1 GHz clock frequency, whereas the A53 processor is designed using a 28 nm FDSOI technology [108] and operates at 1.5 GHz clock frequency. All of the three designs are clock gated and the integrated clock gating cells are inserted automatically by the logic synthesis tool. The 64-point FFT core and Cortex A53 processor clock tree floorplan synthesized by SLECTS are depicted in Fig. 6.6. These clock trees (the clock buffers and nets extracted with RC parasitics) and a counterpart synthesized by a commercial vendor tool are simulated in SPICE. The performance characteristics such as slew, skew, and number of clock buffers as well as power consumption are compared. The results are presented under two scenarios for each circuit. The first scenario represents the slowest corner to evaluate SLECTS under the worst case operating conditions. The second scenario is the evaluation and comparison under scaled supply voltages. These results are presented in the following subsections.



source

(b) Cortex A53 processor clock tree floorplan.

Figure 6.6: Illustration of the clock trees synthesized with SLECTS: (a) 64-point FFT core floorplan, (b) Cortex A53 floorplan.

Circuit	#sinks	#ICGs	Gating%	#gates	Freq	Floorplan($\mu m \times \mu m$)
s38584	1200	263	71.6%	5300	1 GHz	128.06×127.4
64-point FFT	40K	379	7.8%	118K	1 GHz	670.89×670.6
Cortex A53	42K	2400	85.7%	>1M	1.5 GHz	1328.72×1056.8

Table 6.1: Primary characteristics of the test circuits used to evaluate SLECTS.

6.2.1 Results at the Slowest Corner

For 45 nm technology (s38584 and FFT core), worst corner is characterized by slow process parameters, 0.95 V operating voltage, and -40°C temperature. For the 28 nm FDSOI technology (Cortex A53), the slowest corner is represented by slow process parameters, 1 V supply voltage, and 125°C temperature. Slow corner results are presented at two different slew constraints: Case 1 with 70 ps slew constraint for each circuit and case 2 with 30 ps constraint for s38583 and FFT core and 60 ps constraint for Cortex A53 processor. The global skew constraint is 50 ps for s38584 and 100 ps for the larger FFT core and Cortex A53.

Number of clock buffers (for each drive strength), power consumption (switching, net, and leakage), worst slew, and global skew are listed in Table 6.2 for each circuit, for both cases. According to these results, SLECTS consistently inserts less number of total clock buffers as compared to the vendor tool for each circuit. The number of the largest drive strength buffer (X3) is reduced in all cases. In some cases (such as FFT core and s38584 case 2), the number of middle size clock buffer is increased, whereas in for Cortex A53, the number of each clock buffer size is reduced. Specifically, for Cortex A53, SLECTS inserts approximately 13% and 8% less number of clock buffers for, respectively, case 1 and case 2.

For all circuits and cases, SLECTS can either fully satisfy the slew constraint or exhibit negligible violations, whereas vendor tool cannot satisfy the slew constraint

Table 6.2: Comparison of SLECTS with the vendor tool at worst (slowest) corner. X1, X2, X3 refer to the clock buffers
vith increasing drive strength. Skew constraint is 50 ps for s38584, and 100 ps for FFT core and Cortex A53. In Case
l, slew constraint is 70 ps for all three circuits. In Case 2, slew constraint is 30 ps for s38584 and FFT core, 60 ps for
Cortex A53.

			#V1	CV#	¢Λ#	10+01#	Internal	Switching	Leakage	Total	Worst	Global
CIICUIL		(430)		70#	CV#	# IUIAI	(mW)	(mW)	(mW)	(mW)	slew (ps)	skew (ps)
	1.000	Vendor	5	38	14	57	1.12	0.58	5.34e-3	1.71	79.1	24.6
620501		SLECTS	7	37	2	41	1.06	0.52	5.08e-3	1.59	67.5	53.2
+0C0C8		Vendor	29	98	48	175	1.13	0.61	6.97e-3	1.75	40.1	21.4
	Case 2	SLECTS	7	132	7	146	1.02	0.52	6.25e-3	1.55	30.7	56.2
	Coco 1	Vendor	353	1801	878	3032	16.46	16.84	0.07	33.37	82.4	114.5
64 moint DET		SLECTS	216	2144	345	2921	15.24	15.41	0.04	30.69	70.2	133.4
04-puill FF1		Vendor	726	4078	2693	7497	17.81	17.72	0.21	35.74	40.1	64.7
	Case 2	SLECTS	524	4421	1289	6234	15.76	15.62	0.15	31.53	30.1	125.7
	Coco 1	Vendor	795	1465	1509	3769	19.94	41.41	8.34	69.69	88	126
Contag A 52	Case 1	SLECTS	764	1271	1257	3292	17.83	38.84	7.71	64.38	69.4	129.7
COLICA AUD		Vendor	711	2219	2186	5116	19.85	42.33	9.68	71.86	75	108
	7 2000	SLECTS	506	2190	1998	4694	17.97	40.57	8.74	67.28	59.6	117.6

in any of the cases. These results demonstrate the slew-awareness of the proposed methodology. For example, for Cortex A53, in case 1 (70 ps constraint), the vendor tool provides a worst slew of 88 ps whereas SLECTS achieves a worst slew of 69 ps. A similar trend is observed for other circuits.

The worst global skew results of s38584 demonstrate that SLECTS uses the skew budget more effectively by delivering skew results that are closer to the constraint of 50 ps (despite slight violations) whereas the vendor tool delivers skew results significantly lower than the constraint. In the proposed methodology, the effective use of slew and skew budgets reduces the overall clock power, as discussed below. For the larger FFT core and Cortex A53 where skew constraint is 100 ps, both vendor tool and SLECTS exhibit violations, but the delivered worst skew of the vendor tool is closer to the constraint. This result is intuitive since the existing methodologies are primarily delay (skew) driven. For example, for Cortex A53, in case 1, worst skew achieved by the vendor tool and SLECTS are, respectively, 126 ps and 130 ps. In case 2, the worst skews are, respectively, 108 ps and 118 ps. Thus, even though SLECTS exhibits skew violations, the results are still comparable to the vendor tool. These skew violations in SLECTS occur due to the difficulty in producing exact delay values through buffer insertion since the buffer delay strongly depends upon the load of the node and the interconnect length between the pairs. For example, if the interconnect length between the pairs is not sufficiently long, even the smallest size clock buffer does not produce sufficient delay to fix the insertion delay mismatches.

SLECTS methodology lowers the overall power consumption of the clock tree in each circuit, as depicted in Fig. 6.7. An average of approximately 9% reduction in power is achieved. Since slew and skew are simultaneously considered while



Figure 6.7: Power savings in clock tree achieved by SLECTS for both cases.

constructing the tree bottom-up and net splitting is introduced for long wires, less number of clock buffers is required to satisfy the constraints. Thus, both internal and switching power are reduced. SLECTS methodology, therefore, not only satisfies tight slew constraints, but also lowers the overall power consumption of the clock tree.

6.2.2 Results at Scaled Voltages

The behavior of SLECTS methodology under scaled voltages is also investigated. For 45 nm technology (s38584 and FFT core), the voltage is reduced from 1.1 V to 0.7 V. For 28 nm technology (Cortex A53), the supply voltage is scaled from 1.1 V to 0.8 V. Slew constraint is 70 ps for all cases. Skew constraint is 50 ps for s38584, and 100 ps for the larger FFT core and Cortex A53. The overall number of buffers, timing (slew, skew) and power (internal, switching, leakage) results

ndor t is	SLECTS with the ver ngth. Skew constrain hree circuits.	ndor tool at scaled supply voltages. X1, X2, X3 refer to the clock buffers	t is 50 ps for s38584, and 100 ps for FFT core and Cortex A53. Slew	
•	SLECTS with the vendor ngth. Skew constraint is hree circuits.	tool at scaled supply voltage	50 ps for s38584, and 100 p	

							1 I			T. 4.1	117	
Circuit		Cases	#X1	#X2	#X3	#Total	(mW)	Switching (mW)	(mW)	10tal (mW)	slew(ps)	Ulobal skew(ps)
	1117	Vendor	2	45	26	73	0.423	0.577	0.016	1.016	74.9	48.5
	1.1 V	SLECTS	5	37	22	64	0.389	0.523	0.015	0.927	70.1	55.4
	1 007	Vendor	1	46	31	78	0.385	0.478	0.014	0.877	T.TT	49.6
	1.0 V	SLECTS	4	40	24	68	0.359	0.421	0.011	0.791	69.8	61.5
20501	0.01/	Vendor	3	48	33	84	0.294	0.355	0.010	0.659	76.9	45.8
400005	0.9 (SLECTS	4	43	30	LL LL	0.261	0.304	0.009	0.574	70.2	57.8
	10 01	Vendor	5	52	36	93	0.238	0.291	0.007	0.536	78.6	47.9
	0.0 V	SLECTS	ε	43	36	82	0.244	0.248	0.007	0.499	69.8	49.7
	INL U	Vendor	×	55	37	100	0.187	0.231	0.004	0.422	79.9	46.2
	0.1.	SLECTS	2	49	38	89	0.181	0.201	0.003	0.385	70.1	54.1
	1 1 1 1	Vendor	509	1769	1402	3680	16.12	21.85	0.77	38.73	92.9	127.5
	1.1 V	SLECTS	712	1747	892	3351	14.70	19.86	0.72	35.28	70.2	117.8
	1 007	Vendor	511	1785	1521	3817	14.57	17.11	0.53	32.21	91.7	115.9
	1.0 V	SLECTS	654	1839	981	3474	12.59	16.07	0.501	29.16	6.69	121.5
CA actint EET	1000	Vendor	487	1950	1673	4110	10.88	14.32	0.35	25.55	93.3	105.8
04-puill FF1	0.9 (SLECTS	667	2034	1057	3758	10.42	13.08	0.30	23.80	70.4	109.3
	0 017	Vendor	501	2142	1724	4367	9.03	11.08	0.26	20.37	95.4	109.4
	0.0	SLECTS	576	2092	1312	3980	7.64	9.58	0.22	17.43	69.1	106.8
	NL U	Vendor	498	2289	1763	4550	6.62	8.18	0.20	15.00	94.8	100.7
		SLECTS	521	2089	1523	4133	5.74	7.18	0.17	13.10	70.5	105.1
	1 1 1	Vendor	636	1185	649	2470	11.35	37.09	0.17	48.61	96	108
	1.1 V	SLECTS	751	1047	379	2177	9.54	35.22	0.14	44.9	70.1	111.5
	1 01/	Vendor	590	1185	861	2636	9.12	30.59	0.12	39.83	91	132
Contor A52	1.01	SLECTS	458	1102	686	2246	7.24	28.21	0.1	35.55	70.2	124.3
CULICA AUD	10 0	Vendor	658	1207	1245	3110	7.81	24.82	0.09	32.72	90	123
	• ~ ~ ~	SLECTS	688	1014	1007	2709	6.02	22.79	0.07	28.88	70.3	125.7
	0.81	Vendor	1019	1656	1588	4236	6.87	19.77	0.08	26.72	74	113
		SLECTS	983	1575	1317	3875	4.9	17.86	0.06	22.82	70.2	119.9

are listed in Table 6.3 for different voltages. Similar to the worst corner results, SLECTS consistently inserts less number of buffers for each supply voltage. Despite voltage scaling, slew constraint is satisfied, even at the lowest voltages. The global skew results delivered by SLECTS are closer to the vendor tool as compared to the worst corner results. For certain cases, such as Cortex A53 at 1 V, SLECTS achieves a lower global skew (132 ps vs 124 ps). Another interesting observation for Cortex A53 is that the power savings achieved by SLECTS increase from approximately 8% to 15% as the voltage is scaled from 1.1 V to 0.8 V. This result demonstrates the significance of slew driven clock tree synthesis approach for lower operating voltages.

6.3 SLECTS with the Low Swing Flip-Flop

A novel D flip-flop was proposed in Chapter 3. The proposed flip-flop can reliably operate with a low swing clock signal despite a full swing data signal. Simulation results demonstrate that the proposed topology can achieve similar clock-to-Q as that of conventional full swing D flip-flop, thereby preventing any performance degradation in low swing clocking. The power consumption of a conventional full swing flip-flop and the proposed low swing flip-flop is compared in Fig. 6.8 as a function of clock swing. As the clock swing is reduced, the power consumption of the conventional flip-flop significantly increases due to the high short circuit current dissipated by the clock inverters. Up to 45.5% power is saved at a clock swing of 0.7 V. See Chapter 3 for further cell-level results related to the proposed low swing flip-flop.

A slew driven clock tree synthesis algorithm referred to as SLECTS was in-



Figure 6.8: The comparison of power dissipated by conventional full swing flip-flop and the proposed low swing flip-flop as a function of clock swing.

troduced in this chapter to satisfy the skew and slew constraints in voltage-scaled clock trees, while dissipating less power. Contrary to existing approaches that are delay driven, the proposed clock tree synthesis process prioritizes slew over delay since satisfying the slew constraint is highly challenging in nanoscale technologies with higher interconnect resistance and low voltage clock trees.

The significant power reduction achieved by the simultaneous application of the proposed flip-flop and slew aware clock tree synthesis procedure on ISCAS'89 benchmark s38584 and a larger 64-point FFT core is presented in this section. Thus, the results presented in this section represent a clock tree synthesized by the proposed novel algorithm, driving low swing flip-flops, also proposed in this dissertation.



Figure 6.9: The comparison of the clock power of s38584 in two cases: (1) vendor tool synthesized clock tree with conventional full swing flip-flops at the nominal voltage, (2) SLECTS synthesized clock tree with the proposed low swing flip-flops at different clock swings.

6.3.1 ISCAS'89 Benchmark s38584

ISCAS'89 benchmark s38584 is designed in 45 nm technology and has approximately 1200 flip-flops. The circuit is first synthesized by using conventional full swing flip-flops and the clock network is synthesized by a vendor tool at the nominal voltage. The overall clock power (clock network and flip-flops) is determined. Next, the circuit is synthesized by using the proposed low swing flip-flops and the clock network is synthesized by the proposed SLECTS methodology, at different clock swings. The overall clock power in these two cases is compared in Fig. 6.9. Note that SLECTS synthesized clock tree uses the conventional full swing flip-flop at 1.1 V clock swing, since the low swing flip-flop consumes 26.5% more power at this swing, as depicted in Fig. 6.8. For all other clock swings, the proposed flipflop is used. At a clock swing of 0.7 V, approximately 52% power is saved (9 mW vs 4.34 mW). Note that the clock power for this circuit is approximately 65.5% of the overall power consumption. Since the flip-flops consume a significant portion of the overall clock power, replacing the conventional full-swing flip-flop with the proposed flip-flop achieves significant power savings.

In Fig. 6.10, the vendor tool synthesized clock tree with conventional flip-flops is evaluated and compared with the proposed method at different clock swings. Since the power consumed by the conventional flip-flop increases significantly at lower clock swings (due to short circuit current), the overall clock power increases (despite reduction in the power consumed by the clock buffers). In this case, at a clock swing of 0.7 V, the power savings increase to approximately 67% (12.95 mW vs 4.34 mW). Replacing all of the conventional flip-flops with the proposed low swing flip-flop in s38584 design increases the overall area by 32%.



Figure 6.10: The comparison of the clock power of s38584 at different clock swings.

6.3.2 64-point FFT Core

64-point FFT core with approximately 40K sinks designed in 45 nm technology is also evaluated. According to Fig. 6.11, for this larger circuit, approximately 48% power is saved when the proposed low swing flip-flop is used with the clock tree synthesized by SLECTS methodology at a clock swing of 0.7 V. Specifically, the overall clock power for the conventional case is 366.86 mW whereas in the proposed scheme, only 191.9 mW power is consumed. Note that the clock power for this circuit is approximately 48% of the overall power consumption.



Figure 6.11: The comparison of the clock power of 64-point FFT core in two cases: (1) vendor tool synthesized clock tree with conventional full swing flip-flops at the nominal voltage, (2) SLECTS synthesized clock tree with the proposed low swing flip-flops at different clock swings.

If the clock swing is reduced in the conventional case, as depicted in Fig. 6.12, the power savings achieved by the proposed scheme increase to approximately 69% (625.86 mW vs. 191.88 mW) since the power consumed by the conventional flip-flops increases at lower clock swings. The area overhead due to replacing the flip-

flops with the low swing flip-flop is 39% for the 64-point FFT core since the ratio of the flip-flops to overall number of gates is relatively high.



Figure 6.12: The comparison of the clock power of 64-point FFT core at different clock swings.

6.4 Summary

In this chapter, a slew-driven clock tree synthesis (SLECTS) methodology is introduced. In SLECTS, the high interconnect resistance on long wires is managed with a net splitting technique, and a new merging point selection and computation techniques are introduced for power savings. Both slew and skew are methodically considered during the bottom-up synthesis of the clock tree, thereby reducing the overall number of clock buffers. The proposed methodology is shown to be effective not only for satisfying tight slew constraints (where vendor tool fails), but also for reducing clock power, increasingly at low voltages, as demonstrated by an industrial processor in 28 nm FDSOI technology with over 1 M gates. SLECTS was integrated into contemporary academic and industrial CTS tool flows for a slewdriven approach, similar to DME that is popular for the traditional skew-driven CTS approaches. The power analysis of combining SLECTS and low swing flipflop demonstrates significant power savings without performance degradation.

Chapter 7

Conclusion and Future Directions

Low swing clocking is an effective technique to reduce clock network power dissipation. However, existing works on low swing/voltage clock networks are effective primarily for low power applications that do not demand high performance. In this thesis, a novel static D-type flip-flop design, a level shifter for selective low swing clocking, a clock skew scheduling methodology with two different objectives and a slew-driven clock tree synthesis algorithm are proposed to facilitate low swing operation without degrading circuit performance. These contributions are summarized in Section 7.1. Several possible future directions are discussed in Section 7.2.

7.1 Thesis Summary

As technology scales and die area increases, designing a voltage-scaled clock network operating at the same performance has become challenging. Traditional flip-flops cannot reliably work with a reduced swing clock signal. Thus, level shifters are typically inserted at the sinks to restore clock signal to full swing. However, this approach limits the overall power savings since the last stage of a clock network typically has the largest capacitance and therefore benefits the most from low swing clocking. A novel D flip-flop is proposed in Chapter 3. The proposed flip-flop can reliably operate with a low swing clock signal. Simulation results demonstrate that the proposed topology can achieve similar clock-to-Q as that of conventional full swing D flip-flop, preventing any performance degradation in low swing clocking while maximizing power savings.

In high performance clock trees with sufficiently low skew and slew requirement, it may not be practical to lower the clock voltage of the entire clock tree. Selective low voltage clocking has been considered for such situations where part of the clock tree operates at a reduced voltage (to save power) and the rest of the tree operates at nominal voltage to satisfy the performance constraints. Thus, a low overhead level shifter is required to restore clock voltage level. A novel level-up shifter with dual supply voltage is proposed to enable selective low voltage clocking, as described in Chapter 4. The proposed level shifter is compared with conventional cross-coupled topology and level shifters with bootstrapping technique. Simulation results demonstrate the superior performance of the proposed level shifter.

Clock gating is an effective technique to reduce clock network dynamic power dissipation. Thus, modern ICs are typically clock-gated. Existing clock skew scheduling methods cannot effectively consider clock gating when an ICG cell gates multiple registers. In such case, a local clock tree typically exists between the ICG cell and registers gated by this ICG cell, introducing additional and unbalanced clock propagation paths. Furthermore, the *Enable* timing paths of the clock gating cells introduce challenges on satisfying circuit timing constraint, particularly for

low swing clock networks. Therefore, a clock skew scheduling algorithm is proposed in Chapter 5 to maximize circuit performance and increase the timing slack of *Enable* paths. The largest ISCAS'89 benchmark circuits are used to evaluate the proposed algorithm. Simulation results demonstrate that the proposed algorithm can improve circuit performance and facilitate low swing clocking in gated designs.

A slew driven clock tree synthesis algorithm, referred to as SLECTS, is proposed in Chapter 6 to simultaneously satisfy the skew and slew constraints in 1) nanoscale technologies with high interconnect resistance and 2) voltage-scaled clock networks. Contrary to existing approaches that are delay driven, the proposed clock tree synthesis process prioritizes slew over delay since satisfying the slew constraint is highly challenging in low voltage clock trees. The proposed algorithm is evaluated on a large industrial circuit with more than one million gates. Simulation results demonstrate that the proposed algorithm satisfies the slew constraint while reducing the overall clocking power as compared to a vendor tool. The simultaneous application of the proposed flip-flop and slew aware clock tree synthesis procedure demonstrates significant power reduction on an industrial processor.

7.2 Future Directions

In nanoscale technologies, on-chip variation (OCV) has become a challenging problem, particularly for timing closure. Single derating factor based methods have been recently replaced by more advanced and accurate OCV and parametric OCV tables. Since clock networks typically drive a large number of sinks/flip-flops that are distributed throughout the entire die, clock nets run across multiple domains operating with different process-voltage-temperature corners. Thus, clock tree cells significantly suffer from the effects of OCV. Future work on clock tree synthesis can focus on developing a variation-aware clock tree while still satisfying the slew and skew constraints. Clock network insertion delay can be better controlled to minimize the effects of variations. More importantly, these variations can be considered (by utilizing the parametric OCV tables) during the synthesis process to develop a clock tree that is correct by design.

Voltage scaled clock networks suffer from lower noise tolerance. Thus, another important future direction is to evaluate and quantify the effect of low clock voltage on the robustness of the clock tree. This evaluation can be achieved through static noise analysis approaches, similar to static timing analysis that is critical for performance verification. In the next step, clock buffer sizes and interconnect widths can be determined to maximize noise tolerance while still considering clock skew and slew. Thus, similar to variation-awareness, the noise-awareness can also be integrated into the synthesis process.

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